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XXIX. First Analysis of One Hundred and Seventy-seven Magnetic Storms, registered by the Magnetic Instruments in the Royal Observatory, Greenwich, from 1841 to 1857. By GEORGE BIDDELL AIRY, Astronomer Royal.

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1. In a paper which the Royal Society have printed in their Philosophical Transactions for 1862, I gave a series of curves exhibiting to the eye the diurnal inequalities of Terrestrial Magnetism in the three directions of Westerly Force, Northerly Force, and Nadir Force, as inferred from eye-observations and photographic registers at the Royal Observatory from 1841 to 1857. The paper, or the works to which it refers, exhibits also the secular change and the annual inequality through that period, and the lunar inequalities as inferred from the period 1848 to 1857. These results were obtained by excluding the observations of certain days (of which a list was given) on which the motions of the magnetometers were so violent that it was difficult to draw a mean curve through the magnetic curve of the day. In the present paper I propose to give the principal results deducible from the days omitted in the former paper. But before entering into the details of the numerical investigations, I think it desirable to explain the principles upon which both parts of the investigations have been conducted.

2. The methods commonly employed in late years for measuring and classifying the effects of magnetic disturbance have been, in my judgment, very valuable to the science, especially in its earlier stages. But familiarity through many past years with magnetic photograms has strongly impressed me with the feeling that a different method ought now to be employed, taking account of relations of disturbances which perhaps could not be known at the introduction of the ancient method. I may thus describe the general ideas which have guided me:-First, that there is no such thing as a day really free from disturbance, and no reason in the nature of things for separating one or more days from the general series. There is abundant reason for such separation on the ground of convenience of reduction; but when the reduction has been effected by suitable process, the results of the separated days ought to be combined with those of the unseparated days in the formation of general means (the numerical necessity for which I propose to consider in the close of this paper),-the reduction of the separated days serving also to throw great light upon the nature of the acting forces on those days, which forces in all probability are acting, though in different degrees, on other days. Second, that, with our present knowledge of the character of magnetic disturbances. I cannot think myself justified in separating any single magnetic indication, or any series of indications defined only by their magnitude; nor do I entertain the belief that any 4 P MDCCCLXIII.

special value could attach to the results which I might derive from observations from which such indications have been removed. The study of the photograms shows clearly that the successive indications at successive moments of the same day are a connected series; there is no such thing as a sudden display of force in any element; the sharpest salience which is exhibited on a generally smooth curve occupies at least an hour in its development (I believe, never less, although the individual saliences in a continued storm are of shorter duration), and during this time the force has been gradually increasing and gradually diminishing. Under these circumstances, I cannot think it right that I should cut off a part of that salience, with the belief of obtaining results, that can possess any philosophical value, from the part which is left. And I come to the conclusion that each disturbed day must be considered in its entirety, and that our attention ought to be given in the first instance to the devising of methods by which the complicated registers of each of those days, separately considered, can be rendered manageable, and in the next place to the discussion of the laws of disturbance which they may aid to reveal to us, and to the ascertaining of their effects on the general means in which they ought to be included.

3. The discrimination of the classes of days which (on the one hand) are treated by the general process in the "Results of Magnetical Observations, 1859," and of those which (on the other hand) are to be treated by the methods of this Memoir, has been effected entirely by the judgment of the Superintendent of Computations as to the certainty and accuracy with which he could draw a mean line through the disturbed curves. I do however entirely recognize the propriety of defining the "disturbed days" by some numerical limit, when it can be conveniently done: but, the day being defined, I then think that the entire disturbed day or storm ought to be treated as a coherent whole; and that the laws of disturbance and the amalgamation with general means ought to be deduced from it, as already mentioned, without reference to any numerical limit.

4. The records of disturbances from 1848 to 1857 are taken from the photograms; and the value of these, I believe, is unimpeachable. The instruments appear to have been in the highest state of efficiency; I do not think that there is the least doubt on the indications of any disturbed day. And (as the effect of adjustments made expressly for that purpose) the traces of the most violent motions are in general perfectly preserved—an advantage which is possessed, I believe in a peculiar degree, by the photograms of the Royal Observatory. Some sheets may be lost from defects in the paper, defects in the chemical process, &c.; but none, I believe, from rapidity and violence of motion of the magnets. The indications for every salient point of the curves have been translated into numbers which are printed in the "Results of Magnetical Observations" for each year; and those numbers are used as the basis of the following calculations. For the years 1841–1847, in which observations were made by eye, it will be seen in the printed Observations that no opportunity was lost, on the slightest appearance of disturbance, of following most carefully the indications of all the magnetometers: and in fact, as regards both the number of days of such observations and the number of observations on each day, the observations taken are far more numerous than was necessary. The judgment of the Superintendent has been exercised in making such a selection of days and such a limitation of records for each day as should make the adopted register for the period 1841-1847 harmonize well with that for the period 1848-1857.

In the following investigations, whenever one instrument has exhibited such signs of disturbance that its indications were thought unfit for treatment in the former Reductions and are therefore included in this Analysis, the indications of the two other instruments are also included in this Analysis.

5. In deciding on the method of making the disturbed curves more manageable, the following was my train of ideas. As the photographic curve usually consists of a series of lines (very little curved) highly inclined to the time-abscissa and leading alternately upwards and downwards, if each of these lines be bisected and the bisecting points be joined, the joining lines will form a polygon of much less violent character than the original. If these joining lines be bisected and the bisecting points joined, we shall have a polygon of still smoother character, with angles sensibly corresponding to the original times, excepting only the first and the last. If the double process be repeated, the polygon will be still smoother, but wanting points corresponding to the two first and two last observations. And thus we shall have a mean curve containing all the long waves of the original curve, and freed from the irregularities of short period, whose values, however, can be measured. Numerically, each step of the process is represented by taking, for the numerical value of a new ordinate, the arithmetical mean of the numerical values of adjacent ordinates, or, still more easily, by adding the adjacent ordinates, adding the adjacent sums thus formed, and dividing by 4, and repeating this operation. An instance will make this process clear.

Readings for Northerly Force (corrected for temperature) in the Magnetic Storm of 1854, March 6.

The Adopted Numbers are those to be compared with the Original Reading, in order to ascertain what portion of the Original Reading is to be ascribed to Irregularities: and the Adopted Numbers are also to be compared with the Monthly Means deduced from the days of easy reduction, in order to ascertain what portion is to be considered as Wave-Disturbance. Thus we finally obtain the following separation of numbers, whose aggregate represents the Original Reading:—

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Component	parts	of Northerly	Force in	the	Magnetic	Storm	of 1854.	March	6.

Göttingen Time.	Monthly Mean.	Wave-Disturbance.	Irregularities.
h m 1 32 1 50 2 7 2 30 2 44 2 58 3 30 4 5 4 12 4 45 5 23 6 15 6 39 7 6 7 15 7 24 7 32 7 45 8 25 9 17 9 45 10 40 11 23 11 50 12 8 12 20 12 8 13 17 13 45 20 0 22 3	$\begin{array}{r} \cdot 1158\\ 1158\\ 1158\\ 1158\\ 1160\\ 1160\\ 1161\\ 1162\\ 1162\\ 1162\\ 1162\\ 1162\\ 1162\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1163\\ 1164\\ 1164\\ 1164\\ 1164\\ 1164\\ 1164\\ 1164\\ 1164\\ 1164\\ 1161\\ 1156\\ \end{array}$	$ \begin{array}{r} -\cdot 0003 \\ - & 6 \\ - & 7 \\ - & 7 \\ - & 7 \\ - & 5 \\ - & 6 \\ - & 5 \\ - & 1 \\ - & 1 \\ - & 1 \\ - & 1 \\ - & 1 \\ - & 16 \\ - & 18 \\ - & 14 \\ - & 9 \\ - & 4 \\ +\cdot 0002 \\ + & 7 \\ + & 9 \\ - & 4 \\ + & 1 \\ - & 1 \\ - & 1 \\ + & 1 \\ + & 1 \\ \end{array} $	$\begin{array}{c} + \cdot 0014 \\ - \cdot 0013 \\ + 5 \\ - 3 \\ + 4 \\ - 2 \\ 0 \\ - 2 \\ + 2 \\ - 1 \\ + 6 \\ + 2 \\ - 1 \\ + 6 \\ + 2 \\ - 19 \\ + 1 \\ + 5 \\ - 6 \\ + 6 \\ - 14 \\ + 7 \\ - 3 \\ + 4 \\ - 12 \\ + 15 \\ - 3 \\ + 4 \\ - 12 \\ + 15 \\ - 3 \\ + 3 \\ - 6 \\ + 3 \\ - 7 \\ + 8 \\ - 1 \\ + 1 \end{array}$
22 25 22 46 22 55 23 4	1156 1155 1155 1155	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$

The disturbance of Horizontal Force is thus separated into two well-distinguished parts. One part consists of five long waves, alternately - and +. The other part consists of irregularities of short period, which do not show the least symptom of disappearing at the disappearance of the waves, and appear to have nothing in common with them except the connexion of both with the same general Magnetic Storm.

6. For fully understanding the import of these numbers, it will perhaps be necessary to study the succession of numbers in each individual instance. In this First Analysis, I have proceeded, as the first step, to take the means that appear to be most valuable. As regards the Waves, I have taken separately the mean of the wave-disturbances through each wave. But as this quantity gives little information unless taken in conjunction with the time through which it acts, I have multiplied it by the length of the wave in hours; and this product I have distinguished by the technical term *Fluctuation*. The following is now an Epitome of the Magnetic Storm which we have had under consideration.

i and ond or wave.	Length of wave in hours.	Mean Wavo-dis- turbanco.	Fluctuation.	Aggregate Fluctu- ation.	Sum of Hours.	Mean Disturb- ance.	Number of Irregu- laritics.	Mean Pe- riod of Irre- gularity.	
h m h m 0 0 11 1 11 1 12 54 12 54 13 31 13 31 22 51 22 51 23 59	h 11.02 1.88 0.62 9.33 1.13	0007 + 5 - 1 + 5 - 10	$ \begin{array}{c} -\cdot 0077 \\ + & 9 \\ - & 1 \\ + & 47 \\ - & 11 \end{array} $	-•0033	h 23•98	•0001	22 5 2 6 2	h 0·50 0·38 0·31 1·56 0·57	+·0006 8 2 4 4

Epitome of Disturbances of Northerly Force in the Magnetic Storm of 1854, March 6.

The disturbances of Westerly Force and Nadir Force are treated in the same way the values of disturbance, &c. being converted, at convenient stages, into values expressed in terms of whole Northerly Force.

The numbers contained in these Epitomes serve as bases for the investigations which follow. The Epitomes themselves, though greatly reduced from the voluminous calculations on which they are founded, are far too extensive to be included in this Memoir: they will probably be printed in the Greenwich Observations.

7. Treating the Waves as the first subject, I take in the first instance the algebraical aggregate of the Fluctuations for each separate Magnetic Storm. In Table I., the first or longest of the three Tables which follow, every recorded storm is included; and in the second, or Table II., these are all collected to form annual aggregates. But as the days of record do not strictly coincide for the three instruments, partly from accidents in the chemical preparation of the photographic paper, &c., but more particularly from the experimental state of the Vertical-Force Instrument during a part of the year 1848, I have thought it desirable to form Table III. from the observations which are strictly comparable. In regard to the last columns of each department of Table I., and the last lines of Tables II. and III., it will be remarked that the "Fluctuation" is a product of number of hours by Magnetic Disturbance, and therefore, for the Mean Disturbance, the Aggregate of Fluctuations must be divided by the Sum of Hours.

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		Westerly For	xe.		Northerly For	œ.		Nadir Forc	е.
Year, Month, and Day.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregato of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregato of Fluctua- tions.	Algebraic Mean of Disturb- ance.
1841. Sept. 24 25 27 Oct. 25 Nov. 18 19 Dec. 3 14	13.9 22.0 8.2 22.0 17.9 22.8 12.7 10.0	$\begin{array}{r} -0.0022\\ -0.0200\\ -0.0270\\ -0.0270\\ -0.0417\\ -0.0735\\ +0.016\\ +0.088\\ -0.0296\end{array}$	$ \begin{array}{r} - 2 \\ - 9 \\ - 33 \\ - 19 \\ - 41 \\ + 1 \\ + 7 \\ - 30 \\ \end{array} $	12.0 12.9 8.2 22.0 17.9 24.0 12.7 10.0	$\begin{array}{r} -0.0456 \\ -0.0054 \\ -0.0097 \\ -0.0484 \\ -0.025 \\ -0.0276 \\ -0.0205 \\ -0.0130 \end{array}$	$ \begin{array}{r} -38 \\ -4 \\ -12 \\ -22 \\ -7 \\ -12 \\ -16 \\ -13 \\ \end{array} $	14.0 11.3 8.2 20.2 18.0 23.7 10.9 10.0	$\begin{array}{r} -0.0392 \\ + .2580 \\ + .0670 \\ + .0226 \\0323 \\0379 \\ + .0424 \\ + .0621 \end{array}$	$\begin{array}{r} - 28 \\ + 229 \\ + 82 \\ + 11 \\ - 18 \\ - 16 \\ + 39 \\ + 62 \end{array}$
1842. Jan. 1 Feb. 24 Japartian 15 July 1 July 1 Summer 3 Nov. 10 21 Dec. 9	6.7 8.0 7.6 23.1 7.7 13.6 9.7 14.2 12.0 10.0	$\begin{array}{r} -0.0240 \\ -0.0090 \\ +0.0214 \\ +0.0087 \\ +0.0088 \\ -0.523 \\ -0.0033 \\ -0.0340 \\ -0.054 \\ -0.0220 \end{array}$	$ \begin{array}{r} -36 \\ -11 \\ +28 \\ +4 \\ +1 \\ -39 \\ 0 \\ -24 \\ -5 \\ -22 \end{array} $	$\begin{array}{c} 6.7\\ 8.0\\ 7.4\\ 24.0\\ 7.7\\ 13.4\\ 10.0\\ 14.2\\ 12.0\\ 10.0\\ \end{array}$	$\begin{array}{r} + 0.0387 \\ - 0.0400 \\ - 0.0423 \\ - 0.1416 \\ - 0.0178 \\ - 0.0138 \\ - 0.0550 \\ - 0.0710 \\ - 0.0132 \\ - 0.0187 \end{array}$	+58 -50 -57 -59 -23 -10 -65 -50 -11 -19	6.1 8.0 22.2 8.0 13.2 10.0 14.2 12.0 10.0	$\begin{array}{r} + 0.0061 \\ + 0.0014 \\ - 0.0784 \\ - 0.061 \\ + 0.035 \\ + 0.0608 \\ - 0.289 \\ + 0.0312 \\ + 0.0312 \\ + 0.0311 \end{array}$	$\begin{array}{r} + 10 \\ + 2 \\ - 98 \\ - 3 \\ + 17 \\ + 46 \\ - 29 \\ + 13 \\ - 26 \\ + 31 \end{array}$
1843. Jan. 2 Feb. 6 16 24 May 6 July 24 25	10.0 6.0 4.0 11.6 4.4 13.7 6.0	$\begin{array}{r} + 0.0180 \\ + 0.0002 \\ - 0.0044 \\ - 0.129 \\ - 0.216 \\ + 0.145 \\ + 0.210 \end{array}$	+18 0 -11 -11 -49 +11 +35	10.0 4.0 11.6 4.1 13.7 6.0	-0.0180	$ \begin{array}{r} -18 \\ -12 \\ -16 \\ -55 \\ -17 \\ 0 \\ \end{array} $	10.0 11.6 4.2 14.0 5.6	$ \begin{array}{r} -0.0261 \\ + 0.0031 \\ - 0.064 \\ + 0.0140 \\ + 0.0329 \\ \end{array} $	$ \begin{array}{r} - 26 \\ \dots \\ + 3 \\ - 16 \\ + 10 \\ + 59 \end{array} $
1844. Mar. 29 30 Oct. 1 20 Nov. 16 22	15•7 12•0 6•0 10•0 8•0	$ \begin{array}{r} -0.0140 \\ -0.0097 \\ -0.0156 \\ +0.0112 \\ +0.0248 \\ \end{array} $	$ \begin{array}{r} - 9 \\ - 8 \\ -26 \\ \dots \\ +11 \\ +31 \end{array} $	15-7 12-0 6-0 8-0 10-0 8-0	$\begin{array}{r} -0.0305 \\ -0.0126 \\ -0.0198 \\ -0.0224 \\ -0.0280 \\ -0.0196 \end{array}$	$ \begin{array}{r} -19 \\ -11 \\ -33 \\ -28 \\ -28 \\ -28 \\ -25 \end{array} $	16.0 11.6 6.0 8.0 9.7 8.0	$ \begin{array}{r} -0.0448 \\ + .0017 \\ + .0018 \\0904 \\ + .0398 \\0052 \\ \end{array} $	$ \begin{array}{r} - 28 \\ + 2 \\ + 3 \\ -113 \\ + 41 \\ - 7 \\ \end{array} $
1845. Jan. 9 Feb. 24 Mar. 26 Aug. 29 Dec. 3	15.7	$\begin{array}{r} -0.0290 \\ -0.0198 \\ -0.0210 \\ -0.0037 \\ -0.0022 \end{array}$	-29 -13 -15 - 6 - 2	10·0 16·2 14·0 6·1 14·2	$\begin{array}{r} -0.0440 \\ -0.0177 \\ -0.090 \\ -0.024 \\ -0.0667 \end{array}$	-44 -11 -6 -4 -47	10·0 16·2 14·0 6·2 14·2	$\begin{array}{r} + 0.080 \\ - 0.0211 \\ - 0.070 \\ - 0.062 \\ + 0.0439 \end{array}$	+ 8 - 13 - 5 - 10 + 31
1846. May 12 July 11 Aug. 6 7 24 25	22·0 14·0	-0.0009 + .0099 + .0286 0107 0096	-1 +8 +13 -8 -6	10-0 10-0 11-9 22-0 12-0 16-0	$\begin{array}{c} -0.0044 \\ -0.092 \\ -0.0037 \\ -0.013 \\ -0.036 \\ +0.050 \end{array}$	- 4 - 9 - 3 - 1 - 3 + 3 + 3	10-0 3-4 12-0 21-9 16-0 14-2	$\begin{array}{r} -0.0040 \\ -0.0044 \\ -0.015 \\ +0.0051 \\ -0.0160 \\ -0.0071 \end{array}$	$ \begin{array}{r} - 4 \\ - 13 \\ - 1 \\ + 2 \\ - 10 \\ - 5 \end{array} $

TABLE I.—Algebraic Sums of Magnetic Fluctuations (in terms of Horizontal Force) on Days of Great Magnetic Disturbance.

		Westerly For	ce.		Northerly For	°Ce.		Nadir Force	
Year, Month, and Day.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.
1846 (cont ^d). Aug. 28 Sept. 4 5 10 21 22 Oct. 2 7 8 Nov. 26 Dec. 23	8.8 15.9 13.0 13.9 23.8 19.9 14.0 6.0 17.7 12.0 16.2 10.0	$\begin{array}{r} -0.0058 \\ + .0091 \\ + .0056 \\ + .0005 \\0030 \\0286 \\0158 \\0156 \\0073 \\ + .0059 \\0069 \\0160 \end{array}$	$ \begin{array}{r} -7 \\ +6 \\ +4 \\ 0 \\ -1 \\ -14 \\ -11 \\ -26 \\ -4 \\ +5 \\ -4 \\ -16 \\ \end{array} $	8.7 15.8 12.9 13.8 23.8 19.8 14.0 6.0 17.7 11.8 14.6 10.0	$\begin{array}{c} -0.0075 \\ -0.0075 \\ -0.0062 \\ +0.029 \\ -0.0148 \\ -0.0183 \\ -0.0183 \\ -0.0102 \\ -0.0509 \\ -0.0227 \\ -0.0227 \\ -0.0279 \\ +0.0170 \end{array}$	$ \begin{array}{r} -9\\-7\\-5\\+2\\-6\\-9\\-22\\-17\\-29\\-19\\-19\\+17\end{array} $	8.8 16.0 12.3 14.0 23.7 20.0 13.9 6.0 18.0 11.8 16.2 10.0	$\begin{array}{c} -0.0114 \\ + .0208 \\ + .0274 \\ + .0140 \\ + .0292 \\0100 \\ + .0225 \\ + .0060 \\0378 \\ + .0905 \\0002 \\ + .0074 \end{array}$	$ \begin{array}{r} -13 \\ +13 \\ +22 \\ +10 \\ +12 \\ -5 \\ +16 \\ +10 \\ -21 \\ +77 \\ 0 \\ +7 \end{array} $
1847. Feb. 24 Mar. 1 19 April 3 21 May 7 June 24	8.0 20.0 8.0 16.0 6.0 8.0	$\begin{array}{r} -0.0167 \\ + .0082 \\0121 \\0240 \\0046 \\ + .0004 \\ + .0344 \\ + .0109 \end{array}$	$ \begin{array}{c} -17 \\ +10 \\ -6 \\ -30 \\ -3 \\ +1 \\ +43 \\ +27 \end{array} $	10.0 8.0 20.0 8.0 16.0 5.5 8.0	$\begin{array}{c} -0.0110 \\ -0.0047 \\ -0.0846 \\ -0.061 \\ -0.0493 \\ -0.120 \\ -0.032 \end{array}$	$ \begin{array}{r} -11 \\ -6 \\ -42 \\ -8 \\ -31 \\ -22 \\ -4 \\ \end{array} $	9·9 8·0 18·2 8·0 16·0 6·0 10·0	$\begin{array}{r} -0.0030 \\ + .0616 \\0783 \\ + .0264 \\0171 \\ + .0156 \\0100 \end{array}$	$ \begin{array}{r} - & 3 \\ + & 78 \\ - & 43 \\ + & 33 \\ - & 11 \\ + & 26 \\ - & 10 \end{array} $
July 9 Sept. 24 26 27 Oct. 22	 18·0 9·8 10·0 5·8	$ \begin{array}{r} + \cdot 0082 \\ - \cdot 0159 \\ + \cdot 0008 \\ + \cdot 0033 \end{array} $	$ \begin{array}{c} \dots \\ + 5 \\ -16 \\ + 1 \\ + 6 \end{array} $	4·0 18·0 9·8 10·0 5·8	$ \begin{array}{r} - \cdot 0352 \\ + \cdot 0332 \\ - \cdot 0401 \\ - \cdot 0300 \\ - \cdot 0403 \\ \end{array} $	$ \begin{array}{c}88 \\ +18 \\ -41 \\ -30 \\ -70 \end{array} $	4·0 17·0 10·0 9·7 6·0	$ \begin{array}{r} - \cdot 0464 \\ + \cdot 0435 \\ - \cdot 0260 \\ + \cdot 0603 \\ - \cdot 0108 \end{array} $	$ \begin{array}{r} -116 \\ + 26 \\ - 26 \\ + 62 \\ - 18 \\ \end{array} $
23*(1st) 23 (2nd) 24 25 Nov. 22 Dec. 17 18	2.0 23.3 10.0 14.0 22.0	$\begin{array}{r} + \cdot 0091 \\ - \cdot 0025 \\ + \cdot 0137 \\ - \cdot 0093 \\ + \cdot 0120 \\ + \cdot 0157 \\ - \cdot 0120 \end{array}$	$ \begin{vmatrix} + 8 \\ -13 \\ + 6 \\ - 9 \\ + 9 \\ + 7 \\ -10 \end{vmatrix} $	12.0 1.9 23.3 10.0 14.0 22.0 12.0	$\begin{array}{r} - \cdot 0132 \\ - \cdot 0030 \\ - \cdot 2088 \\ - \cdot 0150 \\ - \cdot 0304 \\ - \cdot 0268 \\ - \cdot 0193 \end{array}$	$ \begin{array}{r} -11 \\ -16 \\ -90 \\ -15 \\ -22 \\ -12 \\ -16 \\ \end{array} $	11.6 2.0 23.7 9.5 15.2 14.0	$\begin{array}{r} + \cdot 0988 \\ + \cdot 0016 \\ + \cdot 0538 \\ + \cdot 0654 \\ - \cdot 0421 \\ + \cdot 1260 \end{array}$	$ \begin{array}{r} + 85 \\ + 23 \\ + 69 \\ - 28 \\ + 90 \end{array} $
19 20 1848. Jan. 16		$+ \cdot 0175 - \cdot 0132$	+17 - 7	10·0 18·0	-0.0340	$-91 \\ -32 \\ -33$			
28 Feb. 20 21 22 23 24	16·9 4·0 18·0	$ \begin{array}{r} - \cdot 0210 \\ - \cdot 0192 \\ + \cdot 0047 \\ - \cdot 0043 \\ - \cdot 0113 \\ + \cdot 0335 \\ \end{array} $	-15 -9 +3 -10 -6 +16	19·1 9·1 22·8 4·0 8·6	$\begin{array}{r} + \cdot 0217 \\ - \cdot 0335 \\ - \cdot 0742 \\ - \cdot 0125 \\ - \cdot 0024 \\ - \cdot 0502 \end{array}$	+11 -37 -33 -31 -31	······	·····	······ ······ ·····
Mar. 17 20 April 7 May 18 July 11	3·3 14·2 11·4 9·1 16·4	$\begin{array}{r} + \cdot 0335 \\ + \cdot 0077 \\ - \cdot 0126 \\ + \cdot 0045 \\ - \cdot 0016 \\ - \cdot 0054 \\ + \cdot 0024 \end{array}$	$ \begin{array}{c} +16 \\ +23 \\ -9 \\ +4 \\ -2 \\ -3 \\ +6 \\ -3 \\ +6 \\ -6 \\ -3 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6 \\ -6$	22.8 5.2 11.5 4.1 8.4 19.4	$\begin{array}{r} - \cdot 0503 \\ - \cdot 0067 \\ - \cdot 0309 \\ - \cdot 0074 \\ + \cdot 0105 \\ - \cdot 0415 \\ - \cdot 0271 \end{array}$	$ \begin{array}{r} -22 \\ -13 \\ -27 \\ -18 \\ +12 \\ -21 \\ -21 \\ \end{array} $	······ ······		
Oct. 18	11.5	+ .0024	+ 2	10.6	- ·0271	-26	7.1	-0.0920	

TABLE I. (continued).

* On October 23, 1847, all the observations were interrupted during 10 hours.

		Westerly For	ce.	}	Northerly For	rce.		Nadir Force).
Year, Month, and Day.	Number of Hours.	Algebraic Aggregate of Fluc- tuations.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluc- tuations.	Algebraic Mcan of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluc- tuations.	Algebraic Mean of Disturb- ance.
1848 (cont ^d .) Oct. 23 25 29 Nov. 17 18 Dec. 17	10.6 17.5 16.1 20.0 14.2 9.5	$ \begin{array}{r} -0.0060 \\ -0.0034 \\ -0.0041 \\ -0.0003 \\ -0.266 \\ +0.011 \end{array} $	$ \begin{array}{r} -6 \\ -2 \\ -2 \\ -0 \\ -19 \\ +1 \end{array} $	9·9 18·5 4·4 19·3 10·3 5·5	$ \begin{array}{r} -0.0066 \\ + .0025 \\ .0000 \\1955 \\0201 \\0194 \end{array} $	$ \begin{array}{r} - & 7 \\ + & 1 \\ 0 \\ -101 \\ - & 20 \\ - & 35 \end{array} $	 18·9 4·2 10·3	+ 0.0601 + .0208 0744	$ \begin{array}{c}\\ + 32\\ + 50\\ - 72 \end{array} $
1849. Oct. 30 Nov. 27	22•9 23•1		- 6 + 13	22•8 22•4		$\begin{vmatrix} - & 7 \\ - & 12 \end{vmatrix}$	22·9 	0·3484	-152
1850. Feb. 22 23 Mar. 31 May 7 June 13 Oct. 1 2	23·6 23·9	$ \begin{array}{r} -0.0076 \\ + .0034 \\0104 \\ \dots \\ + .0249 \\ + .0487 \\ + .0401 \end{array} $	$ \begin{array}{r} -3 \\ +1 \\ -4 \\ \dots \\ -10 \\ +21 \\ +17 \end{array} $	23·5 23·3 23·5 23·9 23·4 22·7 23·6	$\begin{array}{r} -0.0088 \\ -0.0327 \\ -0.0375 \\ -0.0021 \\ -0.062 \\ -0.0522 \\ -0.0495 \end{array}$	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	23·3 23·5 23·3 23·7 22·0 22·6	+0.2030 0279 .0000 3882 1188 0098	+ 87 - 12 0 - 164 - 54 - 4
1851. Jan. 16 19 Feb. 18 Sept. 3 4 6 7 29 Oct. 2 28 28 28 29	23.1 18.6 .23.4 24.0 23.0 22.7 23.7 23.1	$\begin{array}{r} -0.0244 \\ + .0175 \\ + .0082 \\ + .0451 \\ + .0465 \\0465 \\0052 \\0550 \\ + .0037 \\ + .0152 \\0307 \\ + .0083 \\0360 \end{array}$	$ \begin{array}{r} -10 \\ +7 \\ +4 \\ +24 \\ +6 \\ -19 \\ -2 \\ +2 \\ +7 \\ -13 \\ +4 \\ -20 \end{array} $	23.4 24.0 23.1 23.4 23.9 23.8 23.9 23.9 23.9 23.9 24.0 22.7 23.4 23.9 22.4	$\begin{array}{r} + 0.0125 \\ + .0328 \\0287 \\0426 \\0232 \\0238 \\0576 \\0474 \\0632 \\0244 \\1264 \\0217 \\0627 \end{array}$	$\begin{array}{r} + & 5 \\ + & 14 \\ - & 12 \\ - & 18 \\ - & 9 \\ - & 10 \\ - & 24 \\ - & 20 \\ - & 26 \\ - & 11 \\ - & 54 \\ - & 9 \\ - & 28 \end{array}$	22.9 23.2 23.4 23.3 23.0 23.4 23.8 22.4 23.6 22.9 22.6 23.2 21.4	$\begin{array}{r} -0.1009 \\1367 \\ +.1382 \\ +.1004 \\ +.1769 \\0508 \\0481 \\3838 \\1364 \\1834 \\ +.0815 \\0950 \\ +.0191 \end{array}$	$\begin{array}{r} - 44 \\ - 59 \\ + 59 \\ + 43 \\ + 77 \\ - 22 \\ - 20 \\ - 171 \\ - 58 \\ - 80 \\ + 36 \\ - 41 \\ + 9 \end{array}$
1852. Jan. 4 19 Feb. 14 15 17 18 19 20 21	22.3 23.7 23.3 23.9 21.0 22.9 20.0	$\begin{array}{r} + 0.0245 \\ + .0073 \\0073 \\ + .0006 \\0021 \\ + .0031 \\0261 \\0078 \\0186 \\00286 \end{array}$	$ \begin{array}{r} +10 \\ +3 \\ -3 \\ 0 \\ -1 \\ +1 \\ -12 \\ -3 \\ -9 \\ +9 \\ \end{array} $	22.0 23.2 23.2 23.7 23.5 23.5 23.5 23.7 23.5 23.7 23.8 23.8 24.0	$\begin{array}{r} + 0.0968 \\0336 \\ + .0771 \\0150 \\0449 \\0587 \\0492 \\0371 \\0604 \\0790 \end{array}$	$\begin{array}{r} + 44 \\ - 14 \\ + 33 \\ - 6 \\ - 19 \\ - 25 \\ - 21 \\ - 16 \\ - 25 \\ - 33 \end{array}$	23.5 22.3 22.1 23.4 23.0 23.9 23.0 23.1 22.5 22.5	$\begin{array}{r} -0.0137 \\ -0.0229 \\ -0.0229 \\ -0.1763 \\ +0.2517 \\ +0.4422 \\ -0.2596 \\ -0.1594 \\ -0.1735 \\ -0.1508 \end{array}$	$\begin{array}{rrrr} - & 6 \\ - & 54 \\ - & 10 \\ - & 75 \\ + & 109 \\ + & 185 \\ - & 113 \\ - & 69 \\ - & 77 \\ - & 67 \end{array}$
April 20 May 19 June 11 16	16·0 6·8 22·5 23·3	$\begin{array}{r} + \cdot 0226 \\ - \cdot 0485 \\ - \cdot 0068 \\ - \cdot 0030 \\ - \cdot 0126 \\ \cdot 0369 \end{array}$	$ \begin{array}{c c} + & 9 \\ - & 30 \\ - & 10 \\ - & 1 \\ - & 5 \\ - & 17 \end{array} $	23.5 23.4 23.5 23.5 23.5 23.5 21.3	$\begin{array}{r} - & 0790 \\ + & 0047 \\ - & 0068 \\ - & 0310 \\ + & 0177 \\ + & 0042 \end{array}$	$ \begin{array}{r} - 33 \\ + 2 \\ - 3 \\ - 13 \\ + 8 \\ + 2 \end{array} $	21·3 13·8 22·3 22·3	$ \begin{array}{r} - & 1300 \\ + & 0595 \\ + & 0605 \\ - & 4354 \\ - & 0302 \\ \end{array} $	+ 28 + 44 - 195 - 14
July 10 Nov. 11 13	23.9	$- \cdot 0362$ + $\cdot 0057$ + $\cdot 0114$	$\begin{vmatrix} -17 \\ + 2 \\ + 5 \end{vmatrix}$	21·3 23·2 23·3	$+ \cdot 0042$ $- \cdot 0235$ $- \cdot 0352$	$\begin{array}{c} + & 2 \\ - & 10 \\ - & 15 \end{array}$	23·0 21·3	$- \cdot 3236$ $- \cdot 1638$	-141 - 77

TABLE I. (continued).

MDCCCLXIII.

MR. AIRY-ANALYSIS OF MAGNETIC STORMS

		Westerly For	ce.		Northerly For	ce.		Nadir Force).
Year, Month, and Day.	Number I of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.
1853. Jan. 10 Mar. 7 8 11 May 2 24 June 22 July 12 July 12 Sept. 1 2 Oct. 1 25 Nov. 9	22.7 23.8 23.0 22.0 23.7 23.3 23.8 23.8 23.8 23.5 23.6 23.5 23.5	$\begin{array}{c} -0.0063 \\ -0.071 \\ -0.073 \\ 0.073 \\ 0.074 \\ +0.092 \\ -0.0157 \\ -0.019 \\ 0.037 \\$	$ \begin{array}{r} -3 \\ -7 \\ -3 \\ -5 \\ -3 \\ +4 \\ -7 \\ -1 \\ \\ +9 \\ +2 \\ \\ -5 \\ +2 \end{array} $	22.6 23.9 23.9 23.9 23.5 23.7 23.6 23.7 23.6 23.7 24.0 24.0 24.0 24.0 23.7	$\begin{array}{c} -0.0200 \\ -0.0224 \\ -0.072 \\ -0.0553 \\ -0.0557 \\ -0.0552 \\ +0.300 \\ -0.029 \\ -0.0029 \\ -0.0032 \\ -0.012 \\ -0.0312 \\ -0.0312 \\ -0.0336 \\ -0.032 \\ -0.0474 \end{array}$	$ \begin{array}{r} -9 \\ -9 \\ -3 \\ -11 \\ -28 \\ -23 \\ +13 \\ -1 \\ -4 \\ \\ -1 \\ -26 \\ -13 \\ -14 \\ -20 \\ \end{array} $	23.8 22.5 23.2 22.9 23.0 23.7 23.2 23.4 23.7 23.5 23.7 24.0 23.5	$\begin{array}{r} +0.3353\\ +\ .5298\\ +\ .3529\\ +\ .3595\\ +\ .3424\\ +\ .2269\\ -\ .1487\\ +\ .0097\\ -\ .0617\\ -\ .0550\\ +\ .0331\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	$\begin{array}{c} & & & & \\ & + 141 \\ + 236 \\ + 152 \\ + 157 \\ + 149 \\ + 96 \\ - 64 \\ + 4 \\ - 26 \\ - 23 \\ + 14 \\ & & \\ & $
Dec. 6 21	23·5 23·5 23·4	$+ \cdot 0037$ + $\cdot 0134$ + $\cdot 0044$	+2 +6 +2	23.7 24.0 23.0	$- \cdot 1079$ $- \cdot 0071$		23·3 23·3 23·3	$+ \cdot 0183$ $- \cdot 1790$	$\begin{vmatrix} - & 35 \\ + & 8 \\ - & 77 \end{vmatrix}$
1854. Jan. 8 20* (resumed) 20 Feb. 16 24 25 Mar. 6 15 16 28 April 10 23 May 25	23.8 23.9 23.8 23.9 23.9 23.9 23.9 23.7 23.5 23.8 23.8 23.9 23.6 23.6	$\begin{array}{r} + 0.0029 \\0043 \\ \hline \\0209 \\0145 \\ + .0049 \\0084 \\0099 \\0034 \\0114 \\0076 \\ + .0103 \\ + .0004 \end{array}$	$ \begin{array}{r} +1\\ -2\\ -9\\ -6\\ +2\\ -4\\ -1\\ -5\\ -3\\ +4\\ 0\\ \end{array} $	23·4 23·5 24·0 23·3 23·9 24·0 24·0 24·0 24·0 23·9 24·0 24·0 24·0 24·0	$\begin{array}{c} + 0.0246 \\0096 \\ \hline \\0337 \\ + .0020 \\ + .0119 \\0033 \\0261 \\0408 \\1271 \\0123 \\0196 \\ + .0176 \end{array}$	$ \begin{array}{c} +11 \\ -4 \\ \\ -14 \\ +1 \\ +5 \\ -11 \\ -17 \\ -53 \\ -5 \\ -8 \\ +7 \end{array} $	23.7 7.0 14.1 23.8 23.7 23.7 23.7 23.9 23.3 23.7 22.7 22.6 23.7 22.6 23.7 23.9	$\begin{array}{r} -0.1089 \\ -0.104 \\ -0.550 \\ -0.1165 \\ -0.1414 \\ +0.812 \\ -0.030 \\ +0.0498 \\ +0.498 \\ +0.498 \\ +0.498 \\ +0.498 \\ +0.0851 \\ -0.0851 \\ +0.0207 \\ -0.0653 \end{array}$	$ \begin{array}{r} - 46 \\ - 15 \\ - 39 \\ - 49 \\ - 60 \\ + 34 \\ - 1 \\ + 21 \\ + 64 \\ - 38 \\ + 9 \\ - 27 \\ \end{array} $
1855. Mar. 12 April 4 July 19 Oct. 18 †	24·0 23·6 23·7	$ \begin{array}{r} -0.0117 \\ -0.0028 \\ -0.0052 \end{array} $	$ \begin{array}{c} -5 \\ -1 \\ - & 2 \end{array} $	23·4 23·6 22·8 24·0	$\begin{array}{r} -0.0506 \\ -0.0108 \\ -0.0263 \\ -0.0477 \end{array}$	$ \begin{array}{r} -22 \\ -5 \\ -12 \\ -20 \end{array} $	23·5 20·3 23·5 23·8	$ \begin{array}{r} -0.2111 \\ -0.0018 \\ -0.0101 \\ +0.1049 \end{array} $	-90 -1 -4 +44
1857. Feb. 26 Mar. 13 May 7 10 Sept. 3 Nov. 12 16 17	22.6 23.2 24.0 23.8 24.0 23.3 21.3 22.8	$\begin{array}{r} + 0.0014 \\ + .0052 \\ + .0207 \\ + .0056 \\0124 \\ + .0163 \\0073 \\0049 \end{array}$	$ \begin{array}{r} + 1 \\ + 2 \\ + 9 \\ + 5 \\ - 5 \\ + 7 \\ - 2 \\ \end{array} $	22.6 24.0 22.1 24.0 23.3 23.3 23.3	$\begin{array}{r} -0.0086 \\ \hline \\ -0.0418 \\ +0.0270 \\ -0.0259 \\ -0.0006 \\ -0.0036 \\ -0.0277 \end{array}$	$ \begin{array}{c} - 4 \\ - 17 \\ + 12 \\ - 11 \\ 0 \\ - 2 \\ - 12 \end{array} $	23•2 22•6 24•0 24•0 	0·1368 ·3191 ·0147 ·4177	- 59 - 141 - 6 - 174
Dec. 16 17	24.0	$- \cdot 0049$ $- \cdot 0021$ $- \cdot 0086$	$\begin{vmatrix} -2 \\ -1 \\ -4 \end{vmatrix}$	22·5 24·0 22·6	$- \cdot 0304$ - $\cdot 0881$	-12 -13 -39	24·0 24·0	•2230 + •0427	-93 + 18

TABLE I. (continued).

* On Jan. 20, 1854, the observations of the Vertical-Force Instrument were interrupted during 3 hours.

+ In 1856 there were no days of Great Magnetic Disturbance throughout the year.

The last figure in the "Algebraic Mean of Disturbance" is in the fourth decimal place of Horizontal Force.

TABLE II.—Algebraic Sums of Magnetic Fluctuations (in terms of Horizontal F	orce) for
each Year from 1841 to 1857, including all days of Record of Great Ma	ignetical
Disturbance.	v

	v	Vesterly For	ce.	N	ortherly For	се.		Nadir Force	•
Year.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregato of Fluctua- tions.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluctua- tions.	Algebraic Mean of Disturb- ance.
1841	129.47	1836	-14	119.63	1827	-15	116-19	+ •3427	+ 29
1842	112.57	1161	-10	113.34	3847	-34	111.74	0132	- 1
1843	55.72	+.0148	+3	49.39	0868	-18	45.40	+ .0175	$+ \frac{1}{4}$
1844	51.74	0033	-1	59.70	1329	-22	59.29	0971	-16
1845	60.00	0757	-13	60.41	- ·1398	-23	60.52	+ .0176	+ 3
1846	244.86	0606	- 2	250.89	- ·1979	- 8	247.99	$+ \cdot 1305$	+ 5
1847	246-75	+.0239	+ 1	246.29	7489	-30	198.75	+ •3193	+16
1848	264.18	0666	- 3	223.83	5274	-24	40.65	- ·0905	- 22
1849	46.00	+.0162	+ 4	45.25	- ·0418	- 9	22.92	- ·3484	-152
1850	141.79	+.0493	+ 3	163.80	- 1890	-12	138.34	3417	- 25
1851	294.04	0830	- 3	305.70	- ·4764		299.17	- ·6190	- 21
1852	364.65	0938	- 3	395.76	- ·2739	- 7	353.07	-1.2159	- 34
1853	327.14	0213	1	402.06	- ·4789	-12	350.67	+2.0150	+ 57
1854	285.10	0619	- 2	285.82	- ·2164	- 8	279.75	— ·3937	- 14
1855	71.37	-•0197	- 3	93.75	— ·1354	-14	91.03	- •1181	- 13
1856	0.00	•0000		0.00	•0000		0.00	•0000	
1857	231.53	+.0139	+ 1	208.37	— ·1997	-10	141.73	-1.0686	- 75
Sum	2926-91	6675		3023.99	-4.4126		2557-21	-1.4636	
Mean Dis- turbance				00146			00057		

TABLE III.—Algebraic Sums of Magnetic Fluctuations (in terms of Horizontal Force) for each Year from 1841 to 1857, including only those days of Great Magnetic Disturbance in which Records were made by the three Instruments.

	v	Vesterly For	ce.	N	ortherly For	ce.		Nadir Force	•
Year.	Number of Hours.	Algebraic Aggregate of Fluc- tuations.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregate of Fluc- tuations.	Algebraic Mean of Disturb- ance.	Number of Hours.	Algebraic Aggregato of Fluc- tuations.	Algebraic Mean of Disturb- ance.
1841 1842	129·47 112·57	1836 1161	-14 -10	119·63 113·34	$- \cdot 1827$ $- \cdot 3847$	-15 -34	116·19 111·74	$+ \cdot 3427$ - $\cdot 0132$	+ 29 - 1
1843	45.72	+.0190	+ 4	45.39	0820	-18	45.40	+ .0175	+4
1844	51.74	0033	-1	51.70	1105	-22	51.29	0067	- i
1845	60.00	0757	-13	60.41	- ·1398	-23	60.52	+ .0176	+ 3
1846	244.86	0606	- 2	240-89	1887	- 8	244 .61	+ .1349	+ 5
1847	202.69	+.0207	+ 1	202.19	- •5453	-27	194.75	+ •3657	+ 19
1848	55.17	0234	- 4	45.74	- •2621	- 58	40.65	0905	- 22
1849	22.92	-·0 129	- 6	22.84	- ·0160	- 7	2 2·92	— ·3484	-152
1850	141.79	+•0493	+ 3	139.88	- •1869	-13	138.34	- •3417	- 25
1851	294.04	0830	- 3	305.70	- •4764	-16	299.17	— ·6190	- 21
1852	341.34	0812	- 2	372-27	- ·2612	- 7	353·07	-1.2159	- 34
1853	304.41	0150	- 1	308.40	- ·3 688	-12	303.72	+1.7238	+ 57
1854	285.10	∙061 9	- 2	285.82	- ·2 164	- 8	279.75	— ·3937	- 14
1855	71.37	·0 197	- 3	70-97	- ·1091	-14	67.58	- ·1080	- 16
1856	0.00	•0000	0	0.00	•0000	0	0.00	•0000	0
1857	141.04	+.0046	0	139-26	— ·1678	-12	141.73	-1.0686	- 75
Sum	2504.23	6428		2524.42	-3.6984		2471.43	-1.6035	
Mean Dis- turbance }	 ∙00026			- •00147			— ·00065		

8. The most remarkable of the results of these Tables is, not only that upon the whole the Algebraic Aggregate of Fluctuations for the Northerly Force is negative (which has been previously recognized), but that it is negative in every separate year. It will be seen in Table I. that on some separate days the Aggregate of Fluctuations is positive, but the number of days is only 22, in opposition to 155 with negative Aggregates.

The Aggregate for the Westerly Force is also negative: and though the different years do not consent in the same way as for the Northerly Force, yet their discordance is not so great as to justify us in setting aside this indication, although there may be greater doubt upon the accuracy of its value. This Aggregate (taken in comparison with that for the Northerly Force) appears to show that, on the whole, the direction of Disturbing Force is 10° to the East of South.

The Aggregate for the Nadir Force appears greater, but it is very uncertain; it might be nearly destroyed by the omission of a single year.

9. These characteristics of the directions of the disturbing forces will appear also in the following enumeration of the instances in which the first and last waves of each Magnetic Storm are affected in different ways. In comparing the numbers it must be borne in mind that, when there is only one wave, that wave is considered, in different places, both as the first and the last.

	Westerly Force.	Northerly Force.	Nadir Force.
Whole number of positive fluctuations	340	177	118
of negative fluctuations	302	277	120
Number of instances in which the first wave is +	106	58	81
in which the first wave is	62	114	64
in which the last wave is $+$	100	15	63
in which the last wave is	68	157	82

Number of Storms beginning with	Westerly Force $+$ and Northerly Force $+$ 35
0 2	Westerly Force + and Northerly Force - $$ 68
beginning with	Westerly Force – and Northerly Force + \cdot 21
beginning with	Westerly Force – and Northerly Force – 40
ending with	Westerly Force $+$ and Northerly Force $+$ 7
ending with	Westerly Force + and Northerly Force - $$ 90
ending with	Westerly Force – and Northerly Force + \cdot \cdot 8
ending with	Westerly Force – and Northerly Force – 58
Number of Storms beginning with	Northerly Force+and Nadir Force + \dots 26
beginning with	Northerly Force+and Nadir Force – 21
beginning with	Northerly Force—and Nadir Force + \cdot
beginning with	Northerly Force—and Nadir Force — \ldots 42
ending with	Northerly Force + and Nadir Force + \dots 6
ending with	Northerly Force+ and Nadir Force $-$
ending with	Northerly Force—and Nadir Force + \cdot \cdot \cdot 57
ending with	Northerly Force—and Nadir Force— 74

10. The following Tables, Tables IV., V., and VI., exhibit the Aggregates of Fluctuations without regard of sign. They are required in order to give information on the Mean Value of Disturbance by Wave in each of the three directions.

TABLE IV.—Absolute Sums, without regard of sign, of Magnetic Fluctuations (in terms of Horizontal Force) on Days of Great Magnetic Disturbance.

	M	Vesterly For	ce.	N	ortherly For	сө.		Nadir Force	•
Year, Month, and Day.	Number of Waves.	Absolute Aggregate of Fluctua- tions.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluctua- tions.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluctua- tions.	Absolute Mean of Disturb- ance.
1841.							_		22
Sept. 24		0.0292	21	1	0.0456	38	1	0.0392	28 228
25	6	•0608	28	2	•0846	66	1	·2580 ·0670	zz8 82
27 Oct. 25	1 4	·0270	33	3 1	·0101 ·0484	12 22	2	•0434	21
Oct. 25 Nov. 18		·0427 ·0961	19 54	1	•0125	22 7	3	·0517	29
19	5	·0214	9	3	·029 2	12	2	•0505	21
Dec. 3	3	.0152	12	3	·0207	16	1	·0424	39
14	2	•0312	31	1	·0130	13	1	•0621	62
1842.							_		
Jan. 1	1	0.0240	36	1	0.0387	58	1	0.0061	10
Feb. 24		•0148	19	1	·0400	50	2	·0044	5
April 14	1	•0214	28	1	•0423	57	1 2	·0784 ·0465	98 21
15		•0311	13	1	·1416	59 02	3	•0137	17
July 1	4	•0100	13	1 5	•0178	23 22	1	·0608	46
2 3	1 2	·0523 ·0283	31 29	1	•0292 •0650	65	2	•0545	55
3 Nov. 10	1	•0340	29 24	1	.0710	50	1	·0185	13
21	2	.0320	27	3	.0248	21	1	•0312	26
Dec. 9	1	•0220	22	3	•0189	19	1	•0311	31
1843.							_		
Jan. 2	1	0.0180	18	1	0.0180	18	1	0.0261	26
Feb. 6	2	·0060	10				•••		
16	1	•0044	11	1	•0048	12	2	•0093	8
24	3	·0131 ·0216	11	3	·0201 ·0226	17 55	2	.0110	26
May 6 July 24	1 2	·0210	49 11	1 2	·0220 ·0247	18	1	·0140	10
July 24 25	ĩ	·0210	35	5	·0026	4	1	•0329	59
1844.									
Mar. 29	2	0.0314	20	3	0.0309	20	1	0.0448	28
30		•0169	14	3	•0126	10	2	·0161	14
Oct. 1		•0156	26	1	·0198	33		·0018 ·0904	3 113
20				1	·0224	28		·0398	41
Nov. 16		•0200	20	1 3	·0280 ·0220	28 28	2	·0092	11
22	1	•0248	31	3	-0220	~0			
1845.		0.0000	20	1	0.0440	44	1	0.0080	8
Jan. 9 Feb. 24		0.0290	29 13	3	.0185	11	1	•0211	13
Mar. 26		•0200	15	3	·0104	7	1	•0070	5
Aug. 29		•0053	9	1	·0024	4	1	•0062	10
Dec. 3		•0310	22	1	•0667	47	1	•0439	31
1846.								0.0119	10
May 12	3	0.0073	7	2	0.0100	10	2 1	0·0118 ·0044	12 13
July 11				2 2	·0118	12	2	•0044	13
Aug. 6		•0209	18	2	·0133	11 4	3	·0123	6
7		•0286	13	7	·0089 ·0036	3	1	·0160	10
24		·0109 ·0096	86	3	•0070	4	1	.0071	5
25 28		•0122	14	3	.0075	9	1	·0114	13
20		0122		<u> </u>	1		I	l	<u> </u>

	7	Vesterly For	сө.	N	ortherly For	ce.		Nadir Force	•
Year, Month, and Day.	Number of Waves.	Absolute Aggregate of Fluctua- tions.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluctua- tions.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluctua- tions.	Absolute Mean of Disturb ance.
1846 (cont ^d)									
Sept. 4		0.0201	13	2	0.0156	10	1	0.0208	13
5	li .	•0148	12	3	·0226	17	2	•0304	23
10	D.	•0187	14	3	•0047	3	1	•0140	10
11		·0342	14	5	•0226	10	3	•0316	13
21	2	•0474	24	3	•0201	10	1	•0100	5
22		•0352	25	3	•0425	30	2	•0645	46
Oct. 2	1	•0156	26	1	•0102	17	1	•0060	10
7	2	•0295	17	3	•0523	29	1	•0378	21
8		•0185	15	3	•0235	20	1	•0905	77
Nov. 26		•0237	14	3	•0281	19	2	•0210	13
Dec. 23	. 1	•0160	16	1	•0170	17	2	•0112	11
1847.		l		ļ			_		
Feb. 24	2	0.0223	22	1	0.0110	11	1	0.0030	3
Mar. 1		•0152	19	2	•0167	21	1	•0616	77
19		•0339	17	2	•0960	48	2	•1269 •0264	70 33
April 3		•0240	30	3	•0067	8	1 2	·0204	13
7		·0224	14	2	•0515	32	1	•0156	26
21	· · · ·	•0028	5	1	•0120	22	1	•0100	10
May 7		•0344	43	2	•0114	14		1	1
June 24	11	•0109	27	i ii		 88	 1	•0464	116
July 9				5	•035 2	106	2	•1277	75
Sept. 24		•0550 •0163	31	1	·1912 ·0401	41	2	•0338	34
26		•0056	17 6	1	•0300	30	ĩ	•0603	62
27 Oct. 22		0.0043	7	2	•0409	71	1	·0108	18
Oct. 22 23*(1s	•••	•0235	20	3	•0564	47	2	·1158	100
23 (2n) 23 (2n)		.0025	13	i	•0030	16	1	•0016	8
23 (21)		.0845	36	5	•2554	110	7	•1144	48
25	11 -	·0103	10	1	•0150	15	1	·0654	69
Nov. 22		.0226	16	2	.0572	41	2	·1057	70
Dec. 17		•0315	14	2	•0552	25	1	·1260	90
18	11 .	·0162	13	1	•0193	16			
19		•0433	43	1	·0910	91			
20	1 10	•0434	24	6	·1277	70		•••••	
1848.									}
Jan. 16		0.0179	12	1	0.0340	33			
28	2	•0306	22	4	·0375	20	•••		
Feb. 20		·0380	17	1	·0335	37	•••	•••••	
21		•0267	16	3	•0962	42			
22		·0045	11	1	•0125	31	•••	•••••	
23		•0235	13	3	•0028	3	•••		
24		•0375	18	3	•0525	23	•••	•••••	
Mar. 17		•0077	23	2	•0093	18 27	•••		
20	11 0	•0208	15	1 2	·0309 ·0084	21	•••		
Apr. 7		•0109	10 11	2	•0123	14	•••		
May 18		·0096 ·0184	11	2	•0689	36			
July 11		•0288	25	3	•0323	30	1	0.0970	136
Oct. 18 23		.0200	19	3	·0234	24			
25		.0158	9	4	.0157	9			
29		•0129	8	î	.0000	ŏ			
~3	··· ~	1	-	-		-		[L

TABLE IV. (continued).

* On October 23, 1847, all the observations were interrupted during 10 hours.

	W	Vesterly Ford	20.	N	ortherly For	ce.	}	Nadir Force	
Year, Month, and Day.	Number of Waves.	Absolute Aggregate of Fluc- tuations.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluc- tuations.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluc- tuations.	Absolute Mean of Disturb- ance.
1848 (cont ^d). Nov. 17 18 Dec. 17	7 3 2	0·0683 ·0276 ·0161	34 19 17	3 3 1	0·1961 ·0271 ·0194	103 26 35	7 1 1	0·0769 ·0208 ·0744	41 50 72
1849. Oct. 30 Nov. 27	3 3	0·0209 ·0295	9 13	2 3	0·0228 ·0280	10 12	1 	0·3484 	152
1850. Feb. 22 23 Mar. 31 May 7 June 13 Oct. 1 2 2	4 6 4 2 1 3	0.0172 .0186 .0214 .0285 .0487 .0421	7 8 9 12 21 18	4 2 1 3 2 1 1	0.0244 .0333 .0375 .0249 .0534 .0522 .0495	10 14 16 10 23 23 21	1 2 1 1 2	0.2030 .0303 .0000 .3882 .1188 .0212	87 13 0 164 54 9
1851. Jan. 16 19 Feb. 18 Sept. 3 4 7 29 Oct. 2 28 Dec. 6 29 28 29	3 4 5 5 7 2 7 6 5 2 4 5 4	0.0432 .0293 .0252 .0473 .0218 .0595 .0462 .0720 .0343 .0772 .0465 .0247 .0420	19 12 11 25 9 25 20 32 14 33 20 11 23	2 2 3 5 3 7 3 5 4 1 3 1	0.0517 0.068 0.0505 0.0522 0.0444 0.0378 1108 0.0972 0.0636 0.0506 1.264 0.0243 0.0627	22 19 22 22 19 15 46 41 27 22 54 10 28	1 1 3 1 3 2 3 1 1 1 3	0·1009 ·1367 ·1382 ·1114 ·1769 ·0648 ·1805 ·3864 ·1370 ·1834 ·0815 ·0950 ·0233	44 59 59 48 77 28 76 172 58 80 36 41 11
1852. Jan. 4 19 Feb. 14 15 17 18 19 20 21 April 20	3 7 4 7 6 7 3 7 3 7	0.0357 .0183 .0217 .0412 .0283 .0277 .0919 .0186 .0370 .0570	15 8 10 17 12 12 43 8 18 24	1 5 3 4 4 5 3 3 3 3	0.0968 .0462 .0823 .0712 .0475 .1041 .1042 .0441 .0660 .0796	44 20 37 30 20 43 44 18 28 33	3 1 4 3 1 1 1 1 1	0.0523 .1206 .0585 .1879 .2525 .4422 .2596 .1594 .1735 .1508	22 54 26 80 110 185 113 69 77 67
April 20 May 19 June 11 July 10 Nov. 11 13	3 1 3 4 2 3	•0487 •0068 •0514 •0310 •0490 •0393 •0386	30 10 23 13 23 17 16	4 3 2 5 2 2 3	•0289 •0140 •0606 •0275 •0336 •0367 •0352	12 6 26 12 15 16 15	1 1 3 1 1	•0595 •0605 •4354 •0660 •3236 •1638	28 44 195 29 141 77

TABLE IV. (continued).

		W	Vesterly For	ce.	N	ortherly For	co.		Nadir Force	•
	, Month, d Day.	Number of Waves.	Absolute Aggregate of Fluc- tuations.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluc- tuations.	Absolute Mean of Disturb- ance.	Number of Waves.	Absolute Aggregate of Fluc- tuations.	Absolute Mean of Disturb- ance.
1	853.									
Jan.	10	3	0.0229	10	3	0.0208	9	•••••		
Mar.	7	8	•0269	11	6	•0302	13	1	0.3353	141
	8	6	•0293	13	5	•0242	10	1	•5298	236
3.6	11			16	5	•0279	12	1	•3529 •3595	152 157
May	2	3 6	·0359	10	1 3	·0657 ·0552	28 23	1	•3424	149
	3 24	7	·0210 ·0280	9 12	5	·0352	38	3	•2273	96
June		3	·0253	11	3	•0259	11	1	.1487	64
July	12	8	·0299	13	3	•0646	27	4	•0777	33
Aug.								1	·0617	26
Sept.	1	7	•0264	11	4	·0838	37	2	·0648	28
- 1	2	5	•0299	13	5	·0738	31	2	•0717	30
Oct.	1				1	•0312	13			
	2				1	•0336	14			•••••
	25	4	•0153	6	3	•0160	7	1	•3093	129
Nov.	9	5.	•0503	21	1	·0474	20	2	•0766	33
Dec.	6	5	•0354	15	1	·1079	45	2	•0633	27
	21	5	•0176	8	3	•0097	42	1	·1790	77
1	854.		}				}	1)		
Jan.	8	3	0.0249	10	2	0.0374	16	1	0.1089	46
	20*	8	·0245	10	3	·0108	4	1	•0104	15
l	20							1	•0550	39
Feb.	16	5	·0219	9	5	•0383	16	1	•1165	49
	24	6	•0335	14	4	•0230	10	3	•1460	62
	25	3	•0135	5	6	•0235	10	2	·1310	55
Mar.	6	4	·0228	10	5	·0145	6	1	•1049	44
	15	9	·0265	11	2	•0407	17	4	•0514	22 21
	16	7	•0294	12	1	•0408	17	1	•0498	64
A	28	4	·0284	12	1	•1271	53		·1451 ·0855	38
April	10 23	6	·0458 ·0233	19 10	4	·0687 ·0334	29 14	2	•0897	38
May		3 6	·0233	10	43	·0188	8	4	.0759	32
may	20	U	0112	J	l v	0100			0,05	
	855.					[1	
	12	5	0.0392	16	2	0.0574	25	1	0.2111	90
April		3	•0248	10	7	·0154	7	2	•0282	14
July	19				2	•0653	29	2	•0719	31 44
Oct.	18	3	•0234	10	2	•0499	21	1	•1049	41
1	857.								1	
Feb.		3	0.0204	9	2	0.0180	8	1	0.1368	59
Mar.		3	·0194	8						
May	7	3	•0689	29	4	·0726	30	1	•3191	141
	10	9	•0118	5	4	•0388	18	2	•0893	37
Sept.	3	6	•0372	15	4	·0515	21	2	•4199	175
Nov.	12	3	·0353	15	4	·0162	7			••••
	16	2	•0271	12	4	·0216	9			••••
n	17	3	•0605	26	3	•0339	15	··· <u>-</u> ···		
Dec.		5	•0405	17	3	•0768	32	1	·2230	93 23
	17	11	•0134	6	1	•0881	39	2	•0543	20

TABLE IV. (continued).

* 1854, Jan. 20. The Vertical-Force observations were interrupted during 3 hours.

† In 1856 there were no days of Great Magnetic Disturbance throughout the year.

The last figure in the "Absolute Mean of Disturbance" is in the fourth decimal place of Horizontal Force.

TABLE V.—Sums, without regard	of sign, of	Magnetic	Fluctuatio	ons (in t	erms of H	ori-
zontal Force) for each Year	from 1841	to 1857,	including	all days	of Record	lof
Great Magnetical Disturbance			0			

			Westerly Fo	orce.	1 1	Northerly F	o rce.		Nadir Fo	rce.
Year.	Number of Storms.	Number of Waves.	Number of Hours.	Absolute Sum of Fluctua- tions.	Number of Waves.	Number of Hours.	Absolute Sum of Fluctua- tions.	Number of Waves.	Number of Hours.	Absolute Sum of Fluctua- tions.
1841	8	25	129.47	·3236	15	119•63	·2641	12	116.19	•6143
1842	10	19	112.57	·2699	18	113.34	•4893	15	111.74	•3452
1843	7	iĭ	55.72	·0990	13	49.39	.0928	7	45.40	•0933
1844	6	10	51.74	·1087	12	59.70	·1357	8	59.29	.2021
1845	5	11	60.00	·1063	9	60.41	·1420	5	60.52	.0862
1846	18	46	244.86	·3632	50	250.89	·3213	28	247.99	·4155
1847	21	100	246.75	•5249	45	246.29	1.2229	30	198.75	1.0719
1848	19	64	264.18	·4356	43	223.83	·7128	10	40.65	·2691
1849	2	6	46.00	·0504	5	45.25	.0508	1	22.92	·3484
1850	7	20	141.79	·1765	14	163.80	·2752	8	138.34	·7615
1851	13	59	294.04	•5692	41	305.70	·8190	24	299.17	1.8160
1852	17	73	364.65	·6422	55	395.76	·9785	27	353.07	2.9661
1853	18	75	327.14	·3941	53	402.06	•8065	24	350.67	3.2000
1854	12	64	285.10	·3057	40	285.82	·4770	25	279.75	1.1701
1855	4	11	71.37	•0877	13	9 3·7 5	·1880	6	91.03	•4161
1856	0	0	0.00	•0000	0	0.00	0000	0	0.00	•0000
1857	10	48	231.53	•3345	29	208-37	•4175	9	141.73	1.2424
Sums	177	642	2926-91	4.7915	455	3023.99	7.3934	239	2557-21	15.0182
Means of Absolute Disturbances } 00164						·00244			•00587	

TABLE VI.—Sums, without regard of sign, of Magnetic Fluctuations (in terms of Horizontal Force) for each Year from 1841 to 1857, including only those days of Great Magnetic Disturbance in which Records were made by the three Instruments.

		1	Westerly Fo	rce.	N	ortherly Fo	orce.	Nadir Force.		
Year.	Number of Storms.	Number of Waves.	Number of Hours.	Absolute Sum of Fluctua- tions.	Number of Waves.	Number of Hours.	Absolute Sum of Fluctua- tions.	Number of Waves.	Number of Hours.	Absolute Sum of Fluctua- tions.
1841	8	25	129.47	•3236	15	119.63	·2641	12	116-19	•6143
1842	10	19	112.57	•2699	18	113.34	•4893	15	111.74	•3452
1843	5	8	45.72	•0886	12	45.39	.0880	7	45.40	·0933
1844	5	10	51.74	·1087	11	51.70	•1133	7	51.29	.1117
1845	5	11	60.00	·1063	9	60.41	•1420	5	60.52	·0862
1846	17	46	244.86	·3632	48	240.89	·3095	27	244.61	•4111
1847	16	83	202.69	•4111	36	202.19	·9497	29	194.75	1.0255
1848	4	16	55.17	·1408	10	45.74	·2749	10	40.65	·2691
1849	ī	3	22.92	.0209	2	22.84	·0228	1	22.92	•3484
1850	6	20	141.79	·1765	11	139.88	·2503	8	138.34	•7615
1851	13	59	294.04	·5692	41	305.70	·8190	24	2 99·17	1.8160
1852	16	69	341.34	·6112	50	372.27	·9510	27	353.07	2.9661
1853	13	72	304.41	•3712	43	308.40	·6930	22	303.72	2.7854
1854	12	64	285.10	•3057	40	285.82	·4770	25	279·7 5	1.1701
1855	3	11	71.37	·0877	11	70.97	•1227	4	67.58	·3442
1856	0	0	0.00	•0000	0	0.00	•0000	0	0.00	•0000
1857	6	37	141.04	·1922	18	139-25	•3458	9	141.73	1.2424
Sums	140	553	2504.23	4.1468	375	2524.42	6.3124	232	2471-43	14.3905
	Means of Absolute Disturbances } •00166			•00250			•00582			

11. In examining the last line of these Tables, it must be borne in mind that the numbers are affected by the constant part of the Disturbance which appears as "Mean Disturbance" at the end of Table III. The value of mean disturbance for Nadir Force (as has been remarked) is uncertain, and that for Westerly Force is small; but that for Northerly Force is important. A constant term -.00147, combined with variable quantities whose mean value is ± 00250 , and whose actual value even at the maximum of its wave will very frequently be far less, will destroy some waves entirely. It will also increase the apparent Mean of Absolute Disturbances, even when the number of waves is not diminished. Thus: suppose, as a simple case, that the pure disturbance is represented by $a \sin \theta$, but that, when affected with a constant term, it is $a \sin \theta - b$. (As has been stated, when a is smaller than b, the addition of -b will make every value -, and will destroy the alternation of + waves and - waves, and thus the just number of waves will be apparently diminished.) When a is greater than b, if Θ be the first value of θ which makes $a \sin \theta - b = 0$, the positive Fluctuation will be found by integrating from $\theta = \Theta$ to $\theta = \pi - \Theta$, and the negative Fluctuation by integrating from $\theta = \pi - \Theta$ to $\theta = 2\pi + \Theta$. The general value of the integral is $-a \cos \theta - b\theta$; the first limited integral is $2a\cos\Theta - b(\pi - 2\Theta)$: the second is $-2a\cos\Theta - b(\pi + 2\Theta)$, or (with sign changed, to make it positive) $+2a\cos\Theta - b(-\pi - 2\Theta)$; and the sum of these, or aggregate of absolute fluctuations, is $4a \cos \Theta + 4b \cdot \Theta$. Now Θ is determined by the condition $a \sin \Theta - b = 0$, or $\sin \Theta = \frac{b}{a}$. If b be small, $\Theta = \frac{b}{a}$ nearly, $\cos \Theta = 1 - \frac{b^2}{2a^2}$ nearly, and the aggregate of absolute fluctuations $= 4a + \frac{2b^2}{a}$. The second term is the increase of the aggregate arising from the introduction of the term b.

If then we conceive the numbers in the last line of Table VI. to be affected with the correction which ought to be introduced in order to neutralize the effect of the large constant term in Northerly Force, it is certain that the number 375 would be considerably increased, and that the number 6.3124 would be considerably diminished. A very extensive examination of details would be necessary to enable us to say what would be the exact proportion of the changes: but it appears to me extremely probable (though at present far from certain) that the corrected Numbers of Waves are sensibly equal, the corrected Absolute Sums of Fluctuations are sensibly equal, and the corrected Means of Absolute Disturbances are sensibly equal, for Westerly Force and for Northerly Force.

The Number of Waves for Nadir Force is less than half that for the other forces; and the Absolute Sum of Fluctuations is about three times as great as that for the others.

12. It would be very important to ascertain any correspondence in the times of the waves in the different directions. I have not yet succeeded in discovering any satisfactory or certain relation.

First, in comparison of the Waves of Westerly and Northerly Forces, the coincidences of times of wave are so rare that it seems evident that nothing can be inferred from the few which can be found. From 1849 to 1857, when the photographic apparatus recorded equally the disturbances at all hours, I do not find one. In a less rigorous examination of the storms from 1841 to 1847, I find that on Nov. 19, 1841, there were contemporaneous waves from $12^{h} 17^{m}$ to $13^{b} 17^{m}$, W. F.+, No. F.+; and on Jan. 1, 1842, when the storm consisted of a single wave, $6^{h} 0^{m}$ to $12^{h} 41^{m}$, the forces were W. F.-, No. F.+. And the second W. F.- on Jan. 16, 1848, corresponds nearly with the sole No. F.-. Sometimes two waves in one direction correspond nearly with one in the other direction: thus in the beginning of the storm 1854, April 10, the W. F.+ from $0^{h} 7^{m}$ to $5^{h} 21^{m}$ and - from $5^{h} 21^{m}$ to $13^{h} 16^{m}$ occupy the same time as No. F.+ from $0^{h} 5^{m}$ to $13^{h} 9^{m}$: but this relation is not supported in the remainder of the same storm. A more frequent relation appears to be, that the evanescence of one wave corresponds with the maximum of the other: thus on February 21, 1852, and March 7, 1853, the waves stand in this order:

	Westerly	Force.	Northerly Force.		
-	Limits of Waves.	Character of Waves.	Limits of Waves.	Character of Waves.	
1852. Feb. 21 1853. Mar. 7	$ \begin{array}{c} 0.27 \\ 4.9 \\ 15.15 \\ 0.10 \\ 4.5 \\ 6.25 \\ 12.20 \end{array} $	+ - + +	$ \begin{array}{c} 0.12\\ 3.14\\ 5.16\\ 23.59\\ 3.13\\ 5.32\\ 7.19\\ \end{array} $		

which relation, however, in the latter instance, is not maintained through the storm. And, generally, this relation does not appear to hold through the whole of any one storm consisting of numerous waves.

13. As the number of Nadir Waves approximates to half the number of Westerly Waves, it might seem worthy of inquiry whether the maximum of Nadir Wave corresponds to a change of Westerly Wave. The following instances have been remarked.

Time of Maximum of Nadir Wave.	Sign of Nadir Wave.	Change of Westerly Wave.	Time of Maximum of Nadir Wave.	Sign of Nadir Wave.	Change of Westerly Wave.
h m 1841. Sept. 25. 3 35 4 17 6 19 1847. Sept. 24. 5 51 10 21 Oct. 23. 5 27 7 1 Oct. 24. 13 4	+++++++++++++++++++++++++++++++++++++++	+ to - - to + + to - + to - - to + + to - + to - + to - + to - + to +	h m 1852. Feb. 18. 4 37 June 11. 14 28 Nov. 11. 8 18 1853. Mar. 8. 6 28 14 24 May 2. 17 35 3. 3 33 24. 10 10	+ + + + + + + + + + + + + + + + + + + +	+ to - - to + + to - + to - + to - - to + + to - - to + + to -
Dec. 17. 6 15 8 13 1851. Sept. 4. 7 19 7. 4 14	+ + +	- to + - to + - to + + to + + to - + + to - + + to - + + to - + + + to - + + + + + + + + + + + + + + + + + +	July 12. 11 37 15 57 Sept. 1. 15 37 2. 5 18	 + +	+ to - - to + + to - + to -
6 30 7 34 10 19 1852. Feb. 18. 2 56	+ - + +	- to + + to - + to - + to -	Oct. 25. 13 47 1854. Apr. 10. 17 56 1857. Dec. 17. 6 10	+ - +	+ to to + + to

I am unable to draw any inference from these.

4 R 2

14. The classification in Article 9 appears to lead to no result as to the effect of connexion of special signs of the first or last waves of the different forces. The inequalities shown in the first Table of Article 9 (of which the difference of numbers of last wave + and numbers of last wave - for the Northerly Force is the most remarkable) are quite sufficient to explain the inequalities in the combinations exhibited in the latter part of Article 9. And, on the whole, the principal conclusions which can be deduced from the examination of the Waves appear to me to be the following :—

That, while on the whole the Westerly Force is -, yet the number of + waves is the greater; and at the beginnings and ends of storms the number of + waves is greater than the number of - waves in a proportion exceeding 3:2.

That, the Northerly Force being on the whole -, in two instances out of three the first Northerly wave is -, and in ten instances out of eleven the last Northerly wave is -.

That, due regard being had to the effect of the constant — Northerly Force, it appears probable that the number of waves and the mean value of wave-disturbance are nearly the same for Westerly Force and for Northerly Force; but

That for the Nadir Force the number of waves is less than one-half the number for the other forces, while the mean value of disturbance is more than double that for the other forces.

15. I now proceed with the Irregularities. The following Tables (VII., VIII., IX.) exhibit their aggregates under the same divisions as those for the Waves. It will be remarked that, from the nature of the process by which the Irregularities are found, their algebraic sum in each storm is sensibly =0; and therefore they are treated here only as numbers without sign.

		1			1		<u></u>	11	N. J'. T.	
			Westerly Ford	e.		Northerly For	·ce.		Nadir Force	
	, Month, d Day.	Number of	Absolute Sum of Coeffi-	Mean Coefficient		Sum of Coeffi-	Mean Coefficient	Number of	Sum of Coeffi-	Mean Coefficient
		Irregu- larities.	cients of Irregularity.	of Irre- gularity.	Irregu- larities.	cients of Irregularity.	of Irre- gularity.	Irregu- larities.	cients of Irregularity.	of Irre- gularity.
	841.					0.0060	10	2	0.0031	15
Sept.		10	0.0133 .1417	13 20	6 73	0.0060 .1226	10 17	61	·1760	29
	25 27	70 6	•0086	14	12	·0090	8	3	.0021	7
Oct.	25	33	·0437	13	36	•0354	10	14	•0157	11
	18	25	•0329	13	28	•0325	12	18	•0208	12
	19	19	•0252	13	26	·0213	8	13	•0139	11
Dec.	3	7	•0134	19	13	•0127	10	3 6	·0018	6
	14	8	•0145	18	9	•0146	16	0	•0072	12
	842.	6	0.0068	11	8	0.0038	5	5	0.0021	4
Jan. Feb	1 24	7	•0132	19	9	.0162	18	3	·0013	4
	14		.0152	13	11	·0168	15	6	•0090	15
	15	20	•0291	15	35	•0373	11	15	•0134	9
July	1	9	•0137	15	15	•0198	13	10	•0113	11
-	2	23	·0349	15	35	·0502	14	10 20	·0134 ·0236	13 12
N T	3	29	•0437	15	42 14	·0502 ·0139	12 10	4	•0230	5
Nov.	10 21	11 14	·0197 ·0132	18 9	15	•0204	14	i	.0008	8
Dec.	9	19	•0209	11	36	•0176	5	6	·0036	6
1	843.		•							
Jan.	2	5	0.0059	12	6	0.0056	9	2	0.0002	3
Feb.	6	3	•0024	8			 3			
	16	7	•0008	1 10	6 37	·0015 ·0166		6	•0041	7
May	24 6	12 17	·0118 ·0206	12	22	•0196	9	9	•0105	12
July	24	4	•0047	12	6	·0058	10	5	·0013	3
ouij	25	14	•0151	11	13	•0141	11	5	•0015	3
	844.					0.0150	~	0	0.0046	E
Mar.	29	21	0.0230	11	24	0·0159 ·0335	7 12	9 7	•0040	5 6
0.4	30	18	•0246 •0056	14 6	29 9	•0070	12	1	•0005	5
Oct.	1 20	9			11	•0113	10	3	·0046	15
Nov.	16	 28	•0290	10	19	•0190	10	9	·0049	5
	22	22	•0234	11	31	•0300	10	9	•0072	8
	845.				9	0.0102	12	4	0.0033	8
Jan.	9		0.0167	11 10	9 26	•0123	12	13	·0072	6
	24		•0163 •0125	10	16	•0124	8	4	.0028	7
	26 29		•0065	3	11	.0087	8	5	·0015	3
Dec.	3		•0698	12	61	•0708	12	27	•0242	9
	846.					0.0100			0.0044	11
	12		0.0161	12	15	0·0130 •0178	9 13	47	·0057	8
July	11			 7	14 35	•0178	15	7	·0036	5
	6	26 64	·0172 ·0207	3	55	•0308	6	15	•0090	6
	7		U ~ V /					18		1
Aug.	7 94			8	9	•0055	6	5	•0015	3
	7 24 25	95	·0075 ·0033	8 7 5	9 5 24	·0055 ·0059 ·0178	12 7	5 2 3	·0015 ·0015 ·0023	3 8 8

TABLE VII.—Absolute Sums, without regard of sign, of Coefficients of Magnetic Irregularity (in terms of Horizontal Force), on Days of Great Magnetic Disturbance.

			Westerly Ford	ж.		Northerly For	·····		Nadir Force).
	, Month, d Day.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irre- gularity.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irre- gularity.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irre- gularity.
1846	6 (cont ^d).									
Sept.	4	26	0.0178	7	29	0.0156	5	5	0.0028	6
•	5	32	·0255	8	36	•0285	8	7	•0093	13
	10	6	•0049	8	6	·0056 ·0378	9 12	3 12	·0008 ·0123	3 10
	11	28	•0311 •0162	11	31 18	•0378	12 9	12	•0041	6
	21 22	23 68	•0771	7	59	•0692	12	28	•0244	
Oct.	22	8	•0089	11	11	.0100	9	3	.0018	9 6
000	7	25	•0343	14	28	.0295	11	3	•0049	16
	8	29	•0213	8	29	·0245	9	5	•0031	6
Nov.	-	28	•0253	9	29	•0235	9	7	•0080	11
Dec.	23	12	•0163	14	9	•0133	17	7	•0039	6
1	847.									
Feb.	847. 24	20	0.0132	7	15	0.0107	7	4	0.0026	7
Mar.	1	42	•0416	10	43	•0384	9	16	·0126	8
	19	49	.0835	17	36	•0518	14	24	•0283	12
April		15	•0214	14	18	•0232	13	3	•0039	13
•	7	19	•0225	12	22	·0306	14	4	•0044	11
	21	12	•0142	12	8	•0095	12	2	•0018	95
May	7	6	•0088	15	4	•0047	12	2	•0010	1
June			•0046	15		•0134	17	 5	•0075	15
July Sept.	9	148	•2666	18	8 128	•3262	26	119	•2192	18
sept.	24 26	12	•0128	11	120	.0142	9	9	.0087	10
	27	16	•0167	10	12	.0124	10	10	.0201	20
Oct.	22	29	.0232	8	30	•0406	14	24	•0157	6
	23*(1st)	86	·1132	13	73	•1332	18	58	•0882	15
	23(2nd)	3	•0016	5	1	•0021	21	2	•0088	44
	24	113	•2034	18	128	•3134	24	94	•1722	18 17
	25	20	•0225	11	17	·0184 ·0462	11	7	•0121	25
Nov.			•0428	13 16	46	.0402	10 15	15 33	·0375 ·0540	16
Dec.	17 18	86 29	·1400 ·0297	10	39 21	•0236	11	11		
	18 19	66	•0937	14	44	•0963	22	•••		
	20	97	•2546	26	64	·2191	34			
	1848.									
Jan.	16	21	0.0570	27	21	0.0381	18	•••		
E.L	28	18	•0361	20 16	19 16	·0422 ·0329	22 21	•••		
Feb.	20 21	35 35	·0573 ·1182	10 34	49	•1857	38	•••		
	2 1 2 2	4	•0099	25	5	•0087	17			
	23		•0283	18	12	·0248	21			
	24	1	•0431	18	21	•0407	19			
Mar.	17	3	•0036	9	7	•0141	20	•••		
	20	28	•0553	20	20	•0470	23	•••		
April		21	•0390	19	9	•0241	27	•••		
May			•0233	12 16	12	·0252 ·0608	21 24			
July Oct.	11	33 21	·0544 ·0675	32	25 18	•0666	37	 14	0.0524	37
000	18 23		•0518	23	19	•0396	21			
	25		•0284	14	22	•0300	14			
	29	11	.0185	17	1	·0018	18	•••		
l				<u> </u>	<u> </u>			1		1

TABLE VII. (continued).

* On Oct. 23, 1847, all the observations were interrupted during 10 hours.

		Westerly Ford	е.		Northerly For	ce.	Nadir Force.			
Year, Month, and Day.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irre- gularity.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irre- gularity.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irre- gularity.	
1848 (cont ^d). Nov. 17 18 Dec. 17	38 17 19	0·1225 ·0272 ·0396	32 16 21	77 17 12	0·2394 •0306 •0213	31 18 18	41 1 14	0.2362 .0008 .0167	58 8 12	
	15	0030	21	12	-0213	10	1.1	-0107	12	
1849. Oct. 30 Nov. 27	19 11	0-0232 -0158	•••	8 7	0·0192 ·0166	•••	4 	0·0046 	12 	
1850.										
Feb. 22 23	27 35	0.0219	8 15	26	0.0356	14 22	5	0.0113	23 43	
Mar. 31	29	·0506 ·0249	9	28 17	·0612 ·0249	15	1	·0129 ·0072	43	
May 7				13	•0174	13				
June 13	13	•0180	14	14	.0202	14	4	•0123	31	
Oct. 1	34	•0384	11	30	•0405	14	8	•0123	15	
2	25	·0390	16	25	•0400	16	7	•0087	12	
1851.										
Jan. 16	43	0.0544	13	36	0.0429	12	4	0.0090	23	
<u>19</u>	37	•0341	9	35	•0420	12	6	•0077	13	
Feb. 18 Sept. 3	22 19	·0297 ·0311	13 16	39	•0410	11 8	20	•0165	8	
Sept. 3 4	29	•0512	18	28 63	·0231 ·0843	13	40 42	·0355 ·0460	9 11	
6	18	•0320	18	40	•0558	14	47	.0388	8	
7	89	·1659	19	106	•1899	18	86	•1367	16	
29	63	•1426	23	122	·1828	15	67	·1115	17	
Oct. 2	33	•0489	15	43	·0602	14	29	•0414	14	
28	24	•0448	19	46	·0509	11	20	•0180	9	
Dec. 6	40	•0697	17	51	•0615	12	30	•0404	13	
28 29	36 47	·0381 ·0463	11 10	37 52	·0313 ·0452	9 9	15 12	·0144 ·0098	10 8	
1852. Jan. 4	38	0.0343	9	22	0.0208	9	18	0.0087	5	
19	31	•0358	12	59	.0540	9	31	•0177	Ğ	
Feb. 14	20	·0255	13	19	.0562	30	17	·0195	11	
15	101	·0987	10	62	•0888	14	53	• 03 98	7	
17	90	·1440	16	92	•1924	21	124	·1354	11	
18	73	•0965	13	66	•1295	20	54	•0576	11	
19	73	·1630	22	71	•1397	20	100	·1789	18	
20	45	•0457	10	60	•0641	11 11	17	·0198 ·0226	12 10	
21 April 20	50 52	·0739 ·0690	15 13	70 52	·0785 ·1515	29	23 41	•0220	10	
May 19	25	•0207	8	36	•0322	~ 3 9	12	•012]	10	
20	3	•0031	10	37	·0466	13	14	.0077	6	
June 11	31	•0573	18	37	•0586	16	32	·0352	11	
16	41	·0373	9	39	·0464	12				
July 10	29	•0352	12	25	•0411	16	15	•0111	7	
Nov. 11 13	37 43	·0483 ·0506	13 12	38 25	·0435 ·0301	11 12	20 12	·0224 ·0080	11 7	
									•	
1853. Jan. 10	19	0.0105	10	16	0.0146	9				
Mar. 7	1	0·0195 ·0423	6	63	•0423	9 7	 11	0.0201	 18	
	00	0420	9		00	7	11	0 0 201	10	

TABLE VII. (continued).

			Westerly Ford	xe.		Northerly For	сө.	Nadir Force.			
	, Month, 1 Day.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irregu- larity.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irregu- larity.	Number of Irregu- larities.	Absolute Sum of Coeffi- cients of Irregularity.	Mean Coefficient of Irregu- larity.	
1853	(cont ^d).						<u>^</u>		0.0175	16	
	ì1				54	0.0411	8	11	0.0175	16 11	
May	2	59 69	0.0367	6	80	·0528	7	15 21	·0165	7	
	3	63	·0391	6	61	•0556 •1206	9 12	37	•0157 •0555	15	
Tune	24	77	·0646	8 7	97 51	•0454	12 9	17	·0170	10	
	22	50 123	·0361	9	129	•1231	10	34	•0524	15	
July	12	120	·1097	9	129	1201	10	8	·0118	15	
Aug.	21 1	42	•0260	6	46	•0418	9	13	·0190	15	
Sept.	2	70	•0665	9	90	•0959	11	36	•0391	11	
Oct.			1	5	12	·0036	3				
000	$ \begin{array}{c} 1 & \dots \\ 2 & \dots \\ \end{array} $	•••••		•••••	9	•0037	4				
	25	22	•0187	9	27	•0156	6	10	·0105	10	
Nov.	9	49	•0407	9	49	·0376	8	19	·0118	6	
Dec.	6	60	•0489	8	41	•0461	11	26	•0321	12	
200.	21	35	•0298	8	28	•0221	8	8	•0067	8	
1	854.									_	
Jan.	8	33	0.0207	6	24	0.0218	9	13	0.0090	7	
	20*	49	•0279	6	35	•0206	6	4	·0023	6	
	20			•••••				4	•0059	15	
Feb.	16		•0460	8	67	•0527	8	26	•0170	7	
	24		•0460	9	67	•0481	7	21	•0175	8	
	25	56	•0405	7	63	•0487	8 6	22	•0208	9	
Mar.	6		•0178	5	37	•0204	6	16	•0216	14	
	15		•0463	8	65	•0425	7	28	•0229	8	
	16	58	•0556	10	69	•0513	7 7 7 9	24	·0188	8 5	
A ·1	28	62	•0591	9	77	•0549	7	49	·0249	0 17	
Aprıl	10	49	•0527	11	79	•0688	9	52	•0357	7 5	
May	23 25	38 38	·0206 ·0229	6 6	49 52	·0322 ·0342	7 6	21 32	·0108 ·0301	9	
. 1	855.										
	12	55	0.0361	6	59	0.0320	5	23	0.0157	7 6	
April		55	.0355	6	53	·0390	7	19	•0111		
July	19				80	•0451	6	21	•0152	7	
Oct.	18	40	•0267	7	60	•0311	5	13	•0111	8	
•	857.		1						•	,	
	26	41	0.0128	3	21	0.0119	6	10	0.0126	13	
Mar.	13	37	•0155	4							
May	7		•0778	9	102	•0883	9	58	·0504	9	
•	10	60	•0196	3	65	•0309	5	13	·0129	10	
Sept.	3	55	•0501	9	92	•0629	7	37	•0296	8	
Nov.	12	47	•0256	5	58	•0292	5				
	16	41	•0265	6	56	• 0 191	3		••••	•••••	
_	17	42	•0329	8	68	·0307	4				
Dec.		66	•0847	13	82	·1496	18	19	•0147	8	
	17	78	•0626	8	93	•0771	8	30	·0221	7	

TABLE VII. (concluded).

In the column "Mean Coefficient of Irregularity," the last figures correspond to the fourth decimal place of Horizontal Force.

* In 1854, Jan. 20, the Vertical Force observations were interrupted during 3 hours.

† In 1856 there were no days of Great Magnetic Disturbance throughout the year.

	W	Vesterly For	ce.	N	ortherly For	·co.	Nadir Force.			
Year.	Number of Storms.	Number of Irregu- larities.	Sum of Coeffi- cients.	Number of Storms.	Number of Irregu- larities.	Sum of Coeffi- cients.	Number of Storms.	Number of Irregu- larities.	Sum of Coeffi- cients.	
1841	8	178	•2933	8	203	·2541	8	120	•2406	
1842	10	150	·2104	10	220	•2462	10	80	•0806	
1843	7	62	•0613	.6	90	•0632	5	27	·0179	
1844	5	98	·1056	6	123	·1167	6	38	·0259	
1845	5	119	·1218	5	123	·1147	5	53	·0390	
1846	17	430	·3585	18	442	·3813	18	130	·1034	
1847	20	905	1.4306	20	772	1.4857	17	431	•6986	
1848	19	408	·8810	19	382	·9736	4	70	•3061	
1849	2	30	•0390	2	15	·0358	1	4	·0046	
1850	6	163	·1928	2 7	153	• 2 398	6	2 8	·0647	
1851	13	500	•7888	13	698	·9109	13	418	·5257	
1852	17	782	1.0389	17	810	1.2740	16	583	·6405	
1853	14	807	•6407	17	910	•8034	15	277	•3404	
1854	12	584	•4561	12	684	·4962	12	312	•2373	
1855	3	150	•0983	4	252	•1472	4	76	·0531	
1856	0	0	•0000	0	0	•0000	0	0	•0000	
1857	10	557	·4081	9	637	•4997	6	167	·1423	
Sums	168	5923	7.1252	173	6514	8.0425	146	2814	3.5207	
Mean Coef- ficient }			·00120			·00123			·0012	

TABLE VIII.—Sums, without regard of sign, of Coefficients of Magnetic Irregularity (in terms of Horizontal Force), for each Year from 1841 to 1857, including all days of Record of Great Magnetical Disturbance.

TABLE IX.—Sums, without regard of sign, of Coefficients of Magnetic Irregularity (in terms
of Horizontal Force), for each Year from 1841 to 1857, including only those days of
Great Magnetic Disturbance in which Records were made by the three Instruments.

		Westerl	y Force.	Norther	ly Force.	Nadir	Force.		
Year.	Number of Storms.	Number of Irregu- larities.	Sum of Coeffi- cients.	Number of Irregu- larities.	Sum of Coeffi- cients.	Number of Irregu- larities.	Sum of Coeffi- cients.		
1841	8	178	•2933	203	•2541	120	·2406		
1842	10	150	·2104	220	·2462	80	•0806		
1843	5	52	·0581	84	-0617	27	•0179		
1844	5.	9 8	·1056	112	·1054	35	•0213		
1845	5	119	·1218	123	·1147	53	•0390		
1846	17	430	·3585	428	·3635	123	•0977		
1847	16	710	1.0480	635	1.1333	426	•6911		
1848	4	95	•2568	124	·3579	70	•3061		
1849	1	19	•0232	8	·0192	4	·0046		
1850	6	163	·1928	140	•2224	28	·0647		
1851	13	500	•7888	698	·9109	418	·5257		
1852	16	741	1.0016	771	1.2276	583	·6405		
1853	13	788	•6212	819	•7404	258	•3111		
1854	12	584	·4561	684	•4962	312	·2373		
1855	3	150	•0983	172	•1021	55	•0379		
1856	0	0	•0000	0	•0000	0	•0000		
1857	6	390	•3076	455	•4207	167	·1423		
Sums	140	5167	5.9421	5676	6·7763	2759	3.4584		
Mean Coefficient			•00115		·00119		•00125		

16. The most striking particulars in the last line of these Tables are the following:First, the almost exact equality of the Mean Coefficients of Irregularity in the threeMDCCCLXIII.

elements. And this remarkable agreement proves that the Irregularities as measured here are real objective facts. For they are measured from photographic sheets in which the scales are very different: on the Westerly and Northerly records, 0.01 of Horizontal Force is represented by 2.87 inches and 2.55 inches, while on the Nadir record 0.01 of Horizontal Force is represented by 0.88 inch. Yet the eye of the Reader of the Photographs has caught the Irregularities when shown on this small scale as certainly as when shown on the larger scale. With reference to their physical import, I think it likely that the equality of Coefficients of Irregularity may hereafter prove to be one of the most important of the facts of observation.

Second, the near agreement in the number of Irregularities for Westerly Force and for Northerly Force.

Third, the near agreement in the number of Irregularities for Nadir Force with half the number of Irregularities for Westerly or for Northerly Force.

17. I have not succeeded in discovering any clear relation between the times of occurrence of Irregularities of Westerly Force and of Northerly Force. They certainly do not coincide. In their intermixture, I cannot assert that an Irregularity of one element always occurs between two of the other element, though there is a general appearance of that law.

18. It appeared to me possible that an Irregularity of Nadir Force might occur at the change between + and - Irregularities of Westerly Force; and the following examination seems to show a certain degree of plausibility in the supposition :—

Day.	Total Number of Nadir Irregularities.	Number of Nadir Irregu- larities corresponding to changes of sign for Westerly Irregularities.
1841. Sept. 25	61	52
1847. Sept. 24	119	76
Oct. 23	60	36
24	94	66
Dec. 17	36	20
1851. Sept. 4	42	26
7	86	68
29	67	50
1852. Feb. 15	53	42
17]24	101
18	54	42
19	100	68
June 11	32	22
Dec. 11	20	14
1853. Mar. 8	11	8
May 2	15	12
3	21	13
24	37	25
July 12	34	25
Sept. 1	13	9
2	36	25
Oct. 25	10	9
Dec. 6	26	23
1854. Feb. 24	21	16
April 10	52	35
1855. Mar. 12	23	16
1857. May 7	58	39
Sept. 3	37	31
Dec. 17	30	21
Total	1372	990

19. The investigations which I had proposed to myself as more peculiarly the object of this paper are now terminated, in so far as their results can be comprehended in tables of numerical values and remarks on the relations between the numbers. But I think it desirable to subjoin Tables tending to exhibit the laws of frequency of the great wave-disturbances and the irregularities, with respect to the months of the year and with respect to the hours of the day.

20. First, for the months of the year. The following numbers are formed by simply collecting from Tables I., IV., and VII. all the numbers arranged in groups under each nominal month. It will be seen at once that the distribution of magnetic storms through the year is so irregular that, even in the long period of seventeen years, no inference can be drawn connecting the Magnetic Storms with the Seasons.

TABLE X.—Aggregates of Fluctuations and Inequalities, arranged by Months, in terms of the Horizontal Force.

	W	Vesterly For	ce.	N	ortherly For	·0e.	Nadir Force.				
Month.	Algebraical Aggregate of Fluctua- tions.	Absolute Aggregate of Fluctua- tions.			Absolute Aggregate of Fluctua- tions.	Sum of Irregulari- ties.	Algebraical Aggregate of Fluctua- tions.	Aggregate of Fluctua- tions. tions.			
January	0435	·3183	·3492	+ .0679	•4827	•3169	5582	•6250	·0662		
February	1425	·6275	1.2093	5521	1.0223	1.3985	1176	2.4732	·5974		
March	- ·1279	·3905	·6038	- ·5193	•6071	·5640	+1.0271	2.0367	·2158		
April	+ .0289	·2635	·3192	- •4074	•4596	•4330	2766	•5416	·1341		
May	0266	·3052	·3533	— ·0554	•4638	•5411	+ .6293	1.9545	•2291		
June	0453	·1471	·1533	- •0224	•1674	·1706	9723	•5841	·0522		
July	- •0598	·2238	•3114	- •2361	•4187	•4414	+ .0109	•4423	·1430		
August	+ .0087	•0875	•0702	— ·0135	•0427	·0859	- •0988	•1 <i>2</i> 94	•0312		
September	— ·1198	•7046	1.1977	- •4614	1.0812	1.3994	- ·1785	2.2337	·9391		
October	+ .0066	·5864	·8836	— ·8129	•9881	1.0282	— ·2781	1.8979	•4866		
November	— ·0431	·6511	•6016	— ·6096	•7150	•6836	·5549	•9893	•3744		
December	- ·1032	•4860	1.0726	— ·7603	•9448	•9799	— ·0 969	1.1105	•2516		

The disproportion of Irregularities to Fluctuations in the Nadir Force, as compared to those in the other Forces, is very remarkable.

21. Secondly, for the hours of the day. For each hour, on a day of storm, the nearest value of wave-disturbance (not of fluctuation) and the nearest value of irregularity were taken from the sheets in which the reductions described in Article 5 were made; and all the numbers thus found were collected for each hour, the + and - values of wave-disturbance being placed in separate columns. Thus the following Table is formed.

4 s 2

Hour		Westerly	Forc.			Northerl	y Force.		Nadir Force.				
of Göt- tingen Time.	Number of Mea-			Sums of Irregu-	Number of Mea-			Number of Mea-	Sums of distur		Sums of Irregu-		
	sures.	+	-	larities.	sures.	+	_	larities.	sures.	+	_	larities.	
0	25	·0201	·0103	·0213	29	·0136	·0717	•0323	5	·0285	·0000	·0090	
1	56	·0558	·0106	•0416	57	•0339	·0726	•0674	19	•0681	•0306	•0236	
2	77	·0658	•0203	•0658	82	·0617	•0900	•0954	33	·1434	•0455	•0370	
3	76	•0881	•0224	•0725	92	·1060	·0807	·1060	40	·1773	·1131	•0563	
4	98	$\cdot 1051$	•0334	·1144	108	·1201	•0823	·1462	63	·3094	·1187	•0774	
5	95	•0831	•0437	·1179	103	·1407	·1019	·1233	60	·2832	•1113	•0681	
6	105	•0752	.0713	·1327	114	·1276	·1291	·1290	74	·3701	•0856	•0794	
78	104	·0593	·1079	·1353	108	•0806	·1422	•1344	77	·3976	•0974	•0915	
8	122	·0331	•1759	•1746	136	·0570	·2171	•1754	79	·3092	·1280	·0853	
9	126	•0276	·1848	·1743	119	·0479	·2393	•1439	80	·2866	·1575	·1169	
10	123	•0165	•2191	·1976	130	·0553	·2612	•1750	86	•2529	•2061	•1241	
11	116	•0267	·1841	•1531	111	•0544	·2747	·1524	77	·2110	·2837	·0889	
12	121	•0278	•2070	•1429	122	•0449	·2917	•1422	74	·1629	·2716	·1007	
13	111	•0277	•2036	·1606	108	•0307	·2470	·1429	63	·1097	•2830	•0799	
14	112	•0442	·1574	•1442	109	•0308	•2897	·1260	74	·1768	•3133	•0941	
15	99	•0601	•1324	·1604	100	•0362	·2194	·1443	59	·1329	•2598	•0717	
16	102	·0537	•0951	·1359	97	·0160	•2428	•1287	59	·0966	•2881	•0825	
17	84	•0695	•0508	•0926	86	·0120	•2137	·1117	54	•0910	•2963	•0619	
18	87	·1016	•0315	•0970	93	•0101	•2043	· 1 169	46	·1010	•2038	•0532	
19	76	·1008	•0193	·0793	85	.0112	•2531	·0990	44	·0830	·1889	•0470	
20	75	•1170	·0107	·0826	81	·0076	•2646	·0713	39	·0614	·1295	·0427	
21	58	•0613	.0083	•0527	65	•0087	·1919	·0694	29	·0619	•0740	·0306	
22	59	·0647	·0179	•0520	69	•0038	•2241	·0694	26	.0355	·0460	·0270	
23	51	•0460	•0214	•0346	57	•0052	•1463	•0441	24	•0491	•0396	•0177	

TABLE XI.—Sums of Wave-disturbances and of Irregularities, arranged by hours of Göttingen Solar Time, in terms of Horizontal Force.

It must be remarked here that the number of measures at 0^{h} is made in this Table unfairly small. This arises partly from the interruptions which are almost unavoidable in the operation of changing the photographic sheets at 0^{h} , and partly from the manner in which the measured quantities have been treated in the discussion of Storms. When a storm has evidently occupied a part of a day, it has been usual to treat by rule the measures of the entire sheet of that day, from 0^{h} to 24^{h} ; and in that process, as is described in the beginning of Article 5, the two first and two last measures are lost; and some of these ought, in a great number of cases, to be referred to 0^{h} . The best value that can be taken for 0^{h} will be the mean of the values for 23^{h} and for 1^{h} .

22. It will be seen that, at the same hour, the mean value of Irregularity is nearly the same for the three Forces, but that, from hour to hour, the mean Irregularities are largest where the number of measures is greatest, that is, where storms are most frequent. In regard to the Wave-disturbance; for Westerly Force, the aggregate is + from 17^h to 6^h, - from 7^h to 16^h; for Northerly Force, the aggregate is + from 3^h to 5^h, - from 6^h to 2^h; and for Nadir Force, the aggregate is + from 23^h to 10^h, - from 11^h to 22^h. In regard to the modification which these Wave-disturbances might be supposed to produce on the laws of Diurnal Inequality, when it is remarked that each of the hours 0^{h} , 1^{h} , 2^{h} , &c. has been repeated 17×365 times, it will be seen that the introduction of these Storm Days into the general mass of observations will in no instance alter the mean Diurnal Inequality by a unit in the fourth decimal place. In a year of very great disturbance, as 1853, they may possibly introduce a correction of one unit, or perhaps two units, in the fourth decimal of some of the Diurnal numbers.

23. The import of the numbers of the last Table will be best seen by the following treatment. If for either of the three directions of force, at any one hour, we form the Algebraic sum of the + and - sums of wave-disturbances, and divide by the number of measures, we obtain the mean wave-disturbance whenever a storm occurs at that hour. If we form the Absolute sum, and divide it similarly, we obtain the double average departure from that mean whenever a storm occurs at that hour. The mean Irregularity is obtained by simple division.

TABLE XII.—Frequency of Storms, mean Wave-disturbance, average departure from the mean, and mean Irregularity, in terms of the Horizontal Force, at each hour of Göttingen Solar Time.

		w	esterly	Force.		Northerly Force.					Nadir Force.				
Hour of Göt- tingen Time.	Fre- quency of Storms.	Mean disturi	wave-	Average departure from Mean. ±	Mean Irregu- larity. ±	Fre- quency of Storms.		an Wave- turbance.	Average departure from Mean. ±	Mean Irregu- larity. 土	Fre- quency of Storms.		ean Wave- sturbance.	Average departure from Mean. <u>+</u>	Mean Irregu- larity. ±
0	54	+ .00	0039	·00061	·00085	57		•00200	·00147	·00112	22	+	·00570	·00285	.00180
1 1	56	+	81	59	74	57	_	68	93	118	19	+	197	260	124
2	77	+ +	59	56	86	82	_	35	93	116	33	1+	297	286	112
3	76	- -	86	73	95	92	+	28	101	115	40	+	161	363	140
4	98	+	73	71	117	108	+	35	94	135	63	+	303	340	123
5	95	+	42	67	124	103	+	38	118	120	60	+	287	329	114
6	105	<u>+</u>	4	70	126	114	_	1	113	113	74	+	385	308	107
7	104	<u> </u>	47	80	130	108		57	103	124	77	+	390	321	119
8	122	_	117	86	143	136		118	101	129	79	+	229	276	108
9	126	-	125	84	138	119		161	121	121	80	+	161	278	146
10	123	_	165	96	161	130		158	122	135	86	+	54	267	144
11	116	 	136	91	132	111		198	148	137	77		94	321	116
12	121		148	97	118	122		202	138	117	74	-	147	294	136
13	111	 _	159	104	145	108	-	20 0	129	132	63	-	275	312	127
14	112		101	90	129	109		238	147	116	74		185	331	127
15	99	_	73	97	162	100	-	183	128	144	59	-	215	333	122
16	102	-	41	73	133	97		234	133	133	59	-	325	326	140
17	84	+	22	72	110	86	-	235	131	130	54	-	380	359	115
18	87	+	81	77	112	93	-	209	115	126	46	- -	224	331	116
19	76	+	107	79	104	85	-	285	155	117	44	-	241	309	107
20	75	+	142	85	110	81	-	317	168	88	39	-	175	245	110
21	58	+	91	60	91	65	-	281	154	107	29	-	42	234	106
22	59	+	79	70	88	69		319	165	101	26	-	40	157	104
23	51	+	48	66	68	57	-	248	133	77	24	+	40	185	74

The Soli-tidal character of the principal characteristics of the occasional Magnetic Storms, as to frequency, magnitude, inequalities of wave-disturbance, and Irregularities, is seen clearly in this Table.

24. I now come to the consideration of the physical inference from these numerical conclusions. And first I would remark that I do not think that they can be reconciled with the supposition of definite galvanic currents or definite magnets, suddenly pro-duced, in any locality whatever, as sufficient to explain the disturbances observed here. On that hypothesis, it would seem necessary to believe that such sudden currents or magnets would produce simultaneous disturbances in the three co-ordinate directions, that, if the long period of a wave permitted some deviation from this rule, yet the short period of an inequality would admit of no such deviation, and that, on any supposition, the number of disturbances in the three directions would be approximately equal. Yet in fact we find that neither in Waves nor in Irregularities is there the least appearance of simultaneity, and that, though there is close equality of numbers between the Westerly and Northerly Forces, yet the Nadir Force (in which the Irregularities are as strongly marked as in the Westerly and Northerly, and the Wave-disturbances much more strongly marked) exhibits less than half the number. These considerations appear to me quite conclusive as showing that the observed disturbances cannot be produced by the forces of any suddenly created galvanic current or polar magnet.

25. To suggest instead of this an imperfect conjecture, based upon grounds so inadequate as those which we can at present use for its foundation, must be a delicate and dangerous, I may almost say an invidious enterprise. Yet the impression of an explanation of broad character, partly definite but generally indefinite, has, in the course of this investigation, forced itself so strongly on my mind, that I should think it wrong to omit to describe it. Its fundamental idea is, that there may be in proximity to the earth something which (to avoid unnecessary words) I shall call a Magnetic Ether; that under circumstances generally, but not always, having reference to the solar hour, and therefore probably depending on the sun's radiation or on its suppression, a current from N.N.W. to S.S.E., approximately, or from S.S.E. to N.N.W. (according to the boreal or austral nature of the ether) is formed in this Ether; that this current is liable to interruptions or perversions of the same kind as those which we are able to observe in currents of air and water; and that their effect is generally similar, producing eddies and whirls, of violence sometimes far exceeding that of the general current from which they are derived.

26. Our powers of observing the two elements to which I have referred for analogy are somewhat different, but both imperfect. We know that in a gale of wind, the direction of the wind is continually changing; the horizontal pressure and the barometric pressure also are continually changing; but the changes are so rapid that we cannot easily determine whether there is any correspondence between them. But, in the storms on a large scale, there is reason to think that some winds are radial, but far more are cyclonic; that in some instances the barometer rises in the centre, but in more it is depressed; and in many instances the disturbance of vertical pressure is enormous (for 1 inch of barometer corresponds to a pressure of about 70 lbs. per square foot). Of water, perhaps the best study is to be found in disturbed tidal currents, as those of the

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Western Islands of Scotland; here, in some places, approximately circular spaces are to be seen which are quiet, but which appear to the eye to be elevated above the rest; in some disturbed places the water is thrown upwards; in other places the sea is whirling round with great speed, in a good circular form, and with a funnel of considerable depth in the centre; in other places, boiling currents are running very fast in opposite directions, though separated by no great space; the general impression however is that of circularity*; great circles and small circles coexisting. Though these circular forms may be more prevalent in one part of the sea than another, they are not fixed, but wander irregularly, sometimes suddenly disappearing, and sometimes as suddenly created anew. In like manner, in the course of a river, travelling funnels may be seen, whose depth sometimes exceeds their breadth.

27. Now it appears to me that if a sentient and reasoning being were immersed either in the air or in the water through which these circles are wandering, he would perceive actions nearly similar to those which we have found to exist in the magnetic storms. The large and slowly-displaced circles would produce Wave-disturbances, slowly changing their direction, and thus having different times of evanescence in the N. and S. direction (on the one hand) and in the E. and W. direction (on the other hand); the smaller circles, in like manner, would produce the rapid Irregularities. And in the relation between E. and W. disturbances and vertical disturbances, there is a point which well deserves attention. When a water-funnel passed nearly over the observer, travelling (suppose) in a N. direction, he would first experience a strong current to the E., afterwards a strong current to the W. (or vice versá), and between these there would be a very strong vertical pressure in one direction, not accompanied by one in the opposite direction; thus he would have half as many vertical as horizontal impulses. This state of things corresponds to the proportion which we have found throughout for the magnetic disturbances, and to the relation found in Article 18. I may also add that the rule at which we have arrived, that the waves of vertical force are few, but that their power, when they do occur, is very great, seems to correspond to what is reported of the whirlwinds of great atmospheric storms; which, violent and even frequent as they may be, occur very rarely at any assigned place.

28. It seems to me that there is so much plausibility in these suppositions as to justify me in expressing a wish that some effort might be made to verify them. The immediate object of observations would be, to ascertain through a locality of considerable extent the times and magnitudes of Wave-disturbances and of Irregularities on the same days throughout, with the view of discovering whether they could be collectively represented as the effects of such travelling vortices as I have suggested. In regard to the extent of the locality, I should think that a portion of the Continent of Europe would suffice, and that five or six magnetic observatories would decide the points under inquiry. In regard to the mode of observation, though eye-observation is, for a limited time, the most accurate, yet self-registering record is the only method which can insure the

* I have been upon these currents, and in close proximity to these whirlpools.

observation of all that is required; only, I would specially observe, it is indispensable that eye-observations be used to check the zeros of time and of measure, and that the photographic traces be so strong that they will not be lost in rapid motions of the magnet. In regard to the mode of primary reduction, I imagine that the method followed in this Memoir (with such small alterations as experience may suggest) will be found best.

** The computations for the "Diurnal Inequalities" were performed by computers under the immediate superintendence of Mr. JOHN LUCAS; some portions of them were revised and corrected by JAMES GLAISHER, Esq., F.R.S., Superintendent of the Magnetical and Meteorological Department of the Royal Observatory. The curves were drawn under Mr. GLAISHER'S superintendence by Mr. W. C. NASH, and reduced to scale by Mr. JAMES CARPENTER, Assistant in the Astronomical Department of the Royal Observatory. The computations of the present Memoir were made under the superintendence of Mr. GLAISHER, by Mr. NASH and junior computers.

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